



# Radiofrequency Measurements

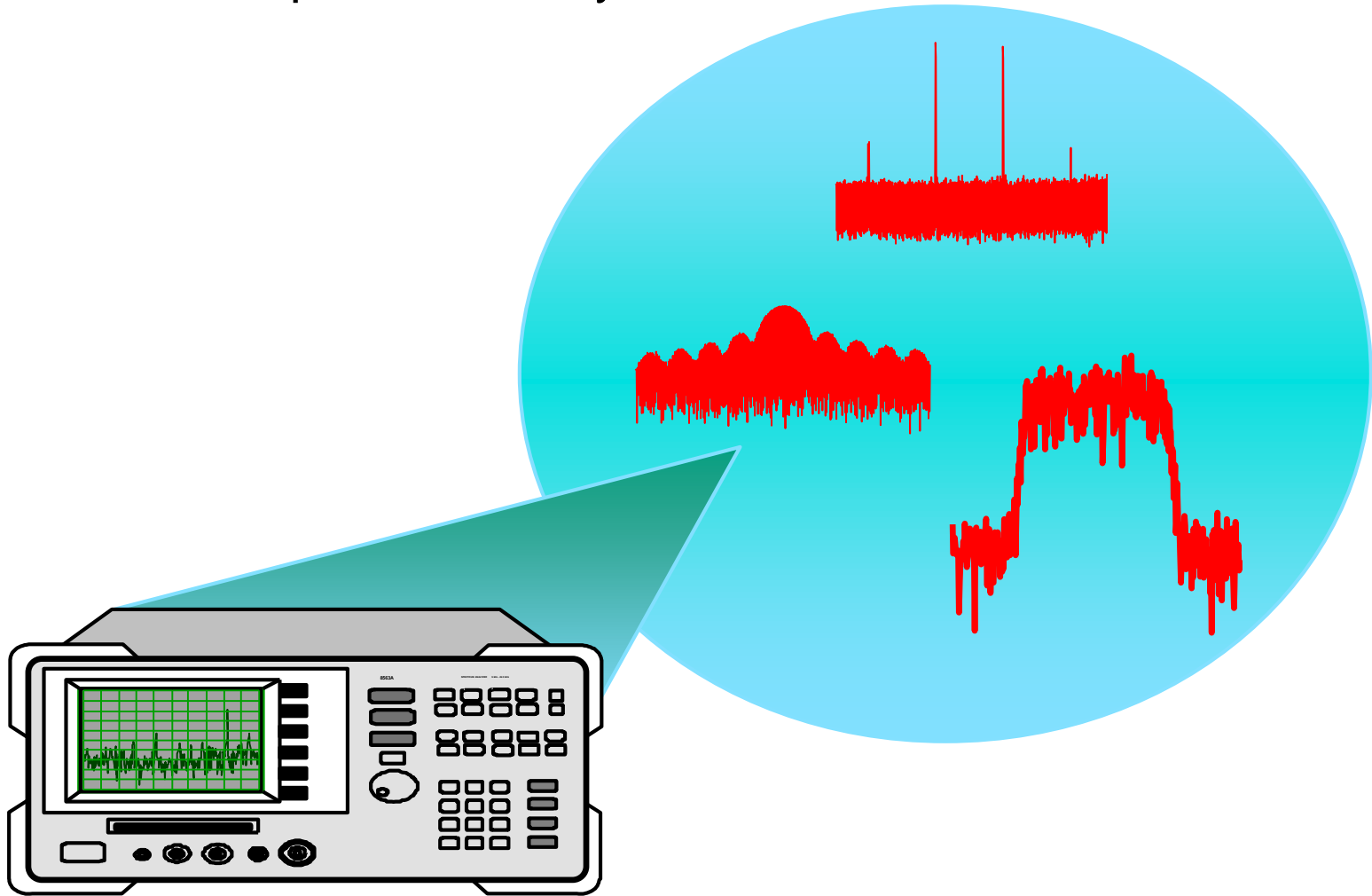
## Spectrum Analyzers

The next slides material is taken from

- AGILENT “**Spectrum Analysis Basics**”
- TEKTRONIX’ “**Fundamentals of Real-Time Spectrum Analysis**”
- ROHDE&SCHWARZ “**Key points of real time**”

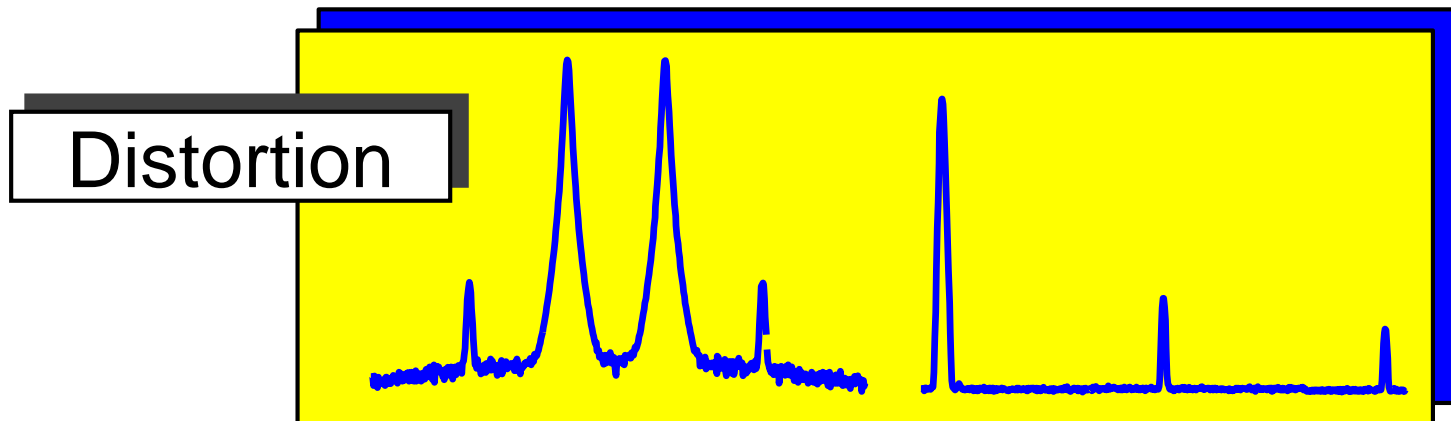
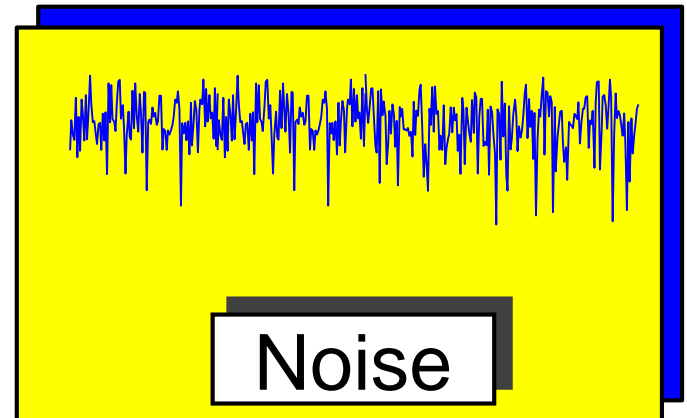
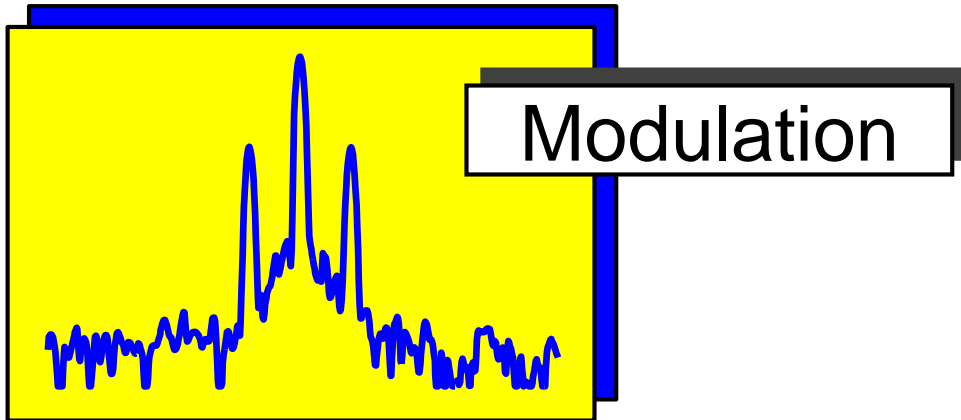
# Overview

What is Spectrum Analysis?



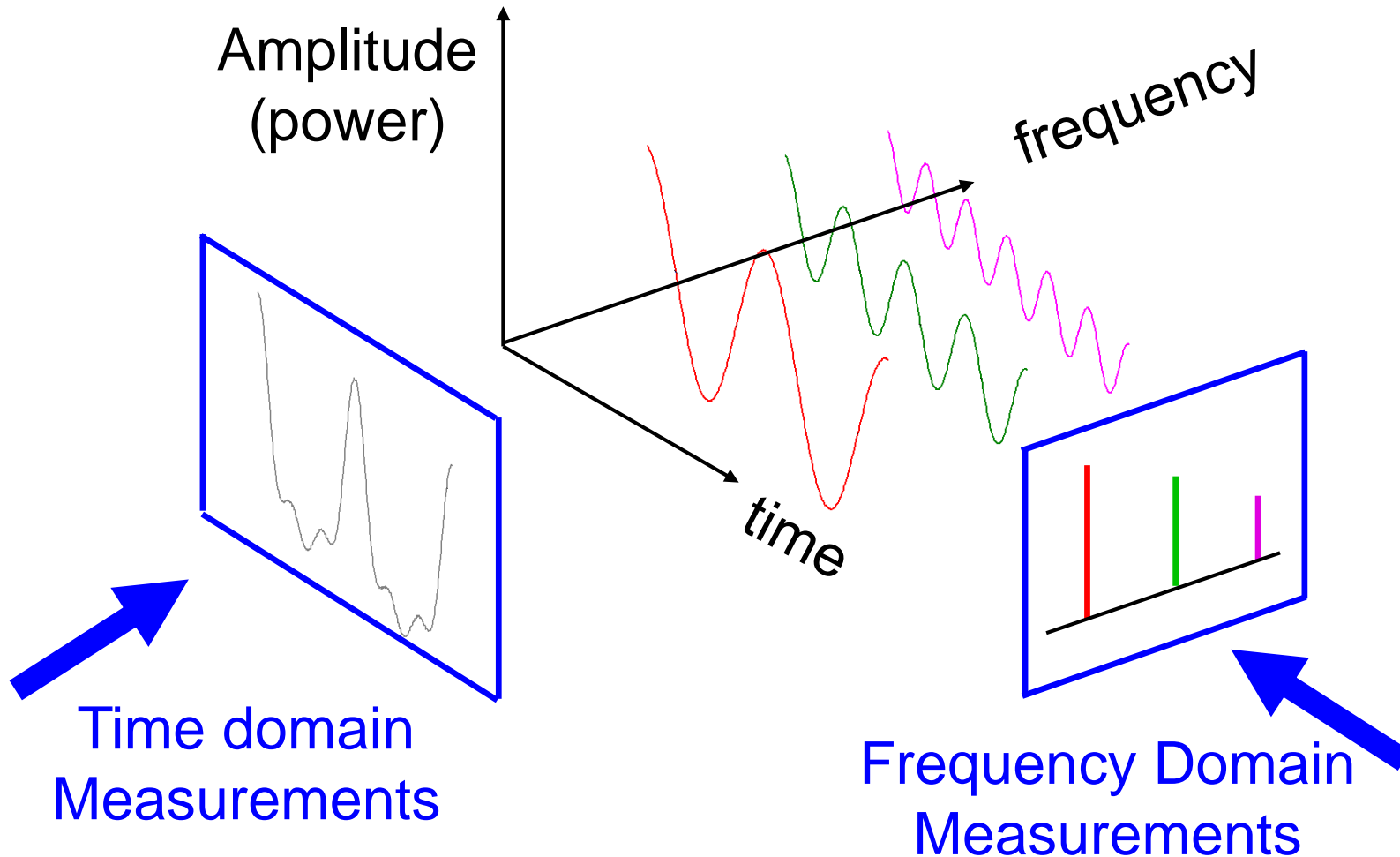
# Overview

## Types of Tests Made



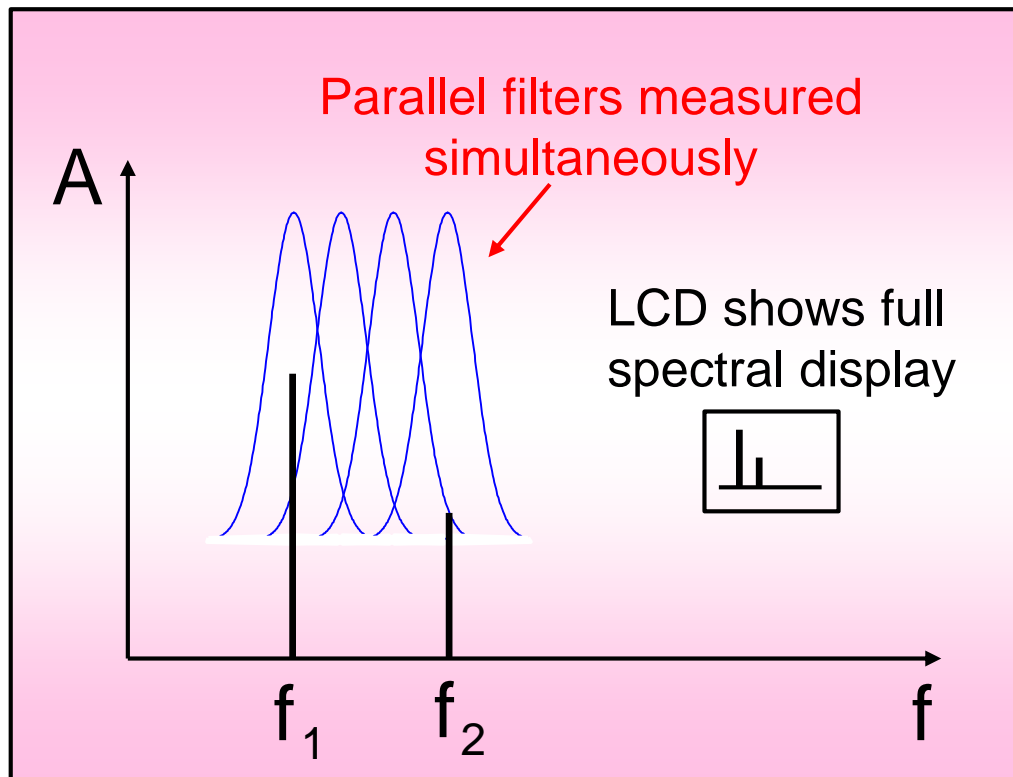
# Overview

## Frequency versus Time Domain



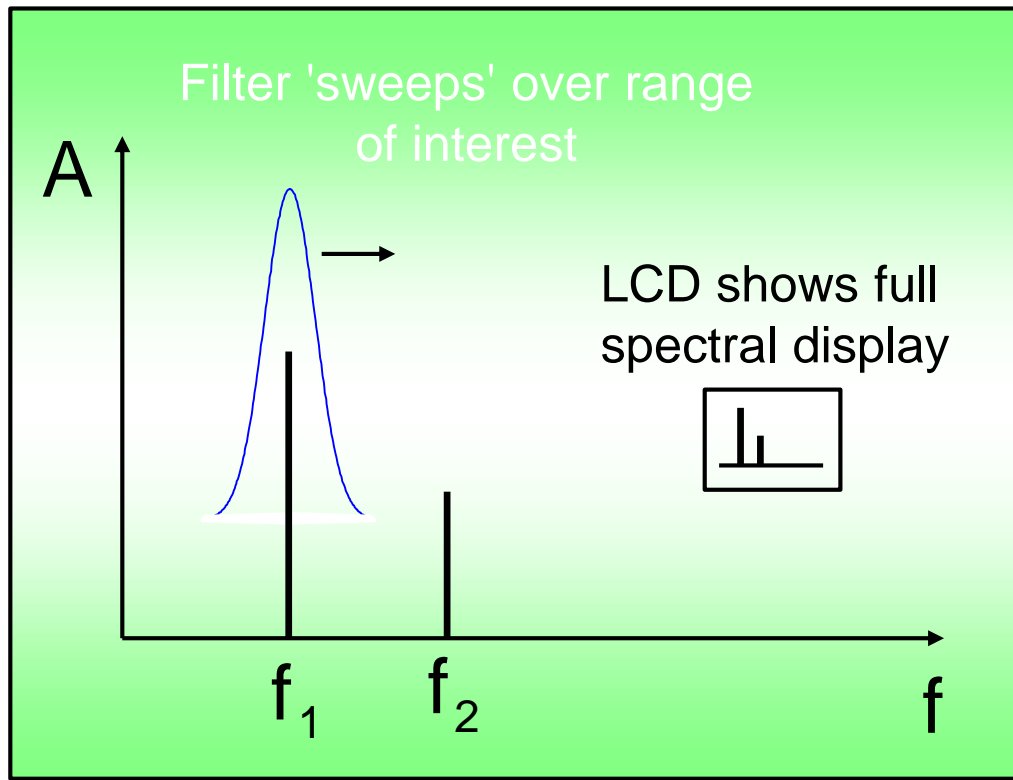
# Overview

## Different Types of Analyzers

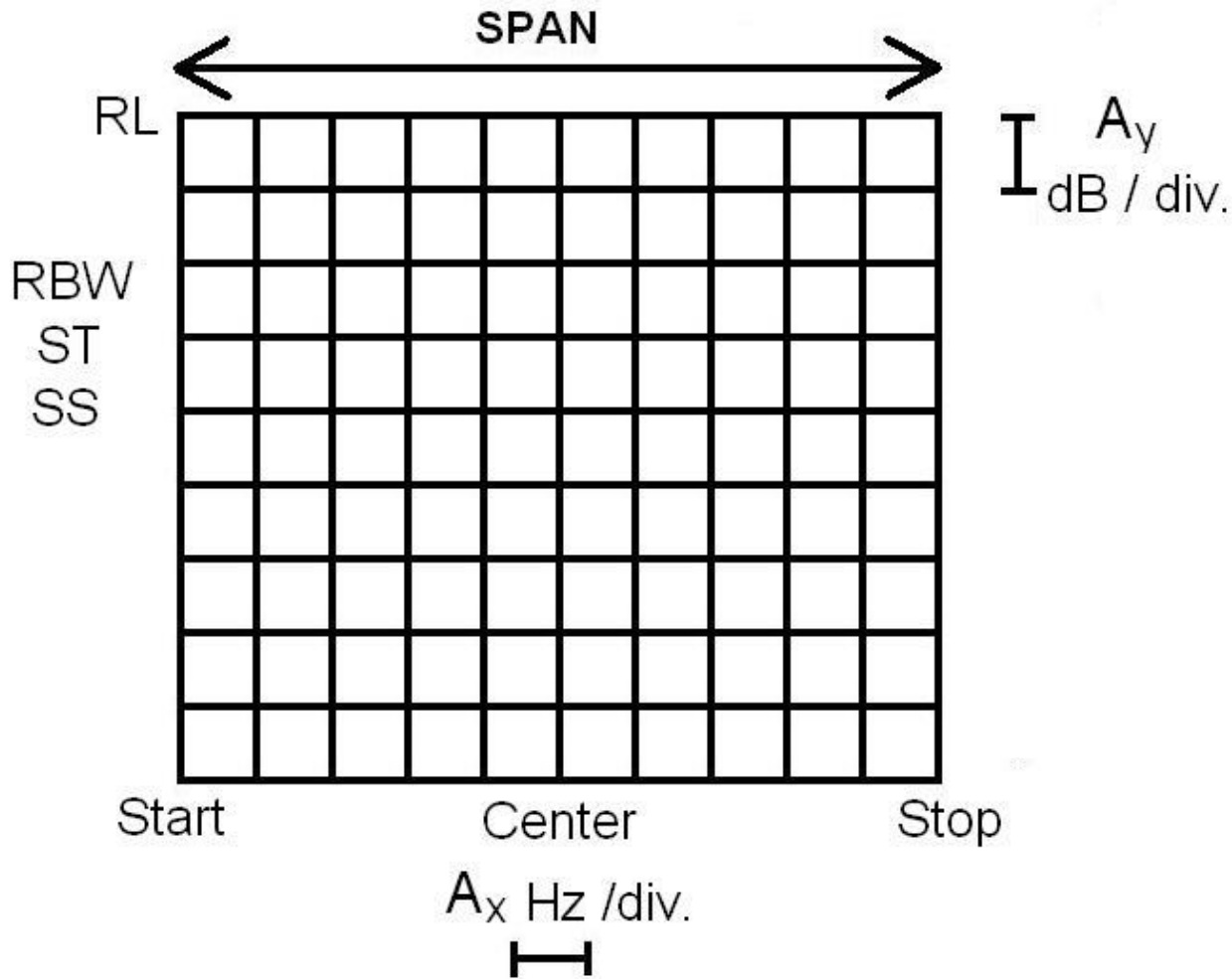


# Overview

## Different Types of Analyzers



# Screen Parameters

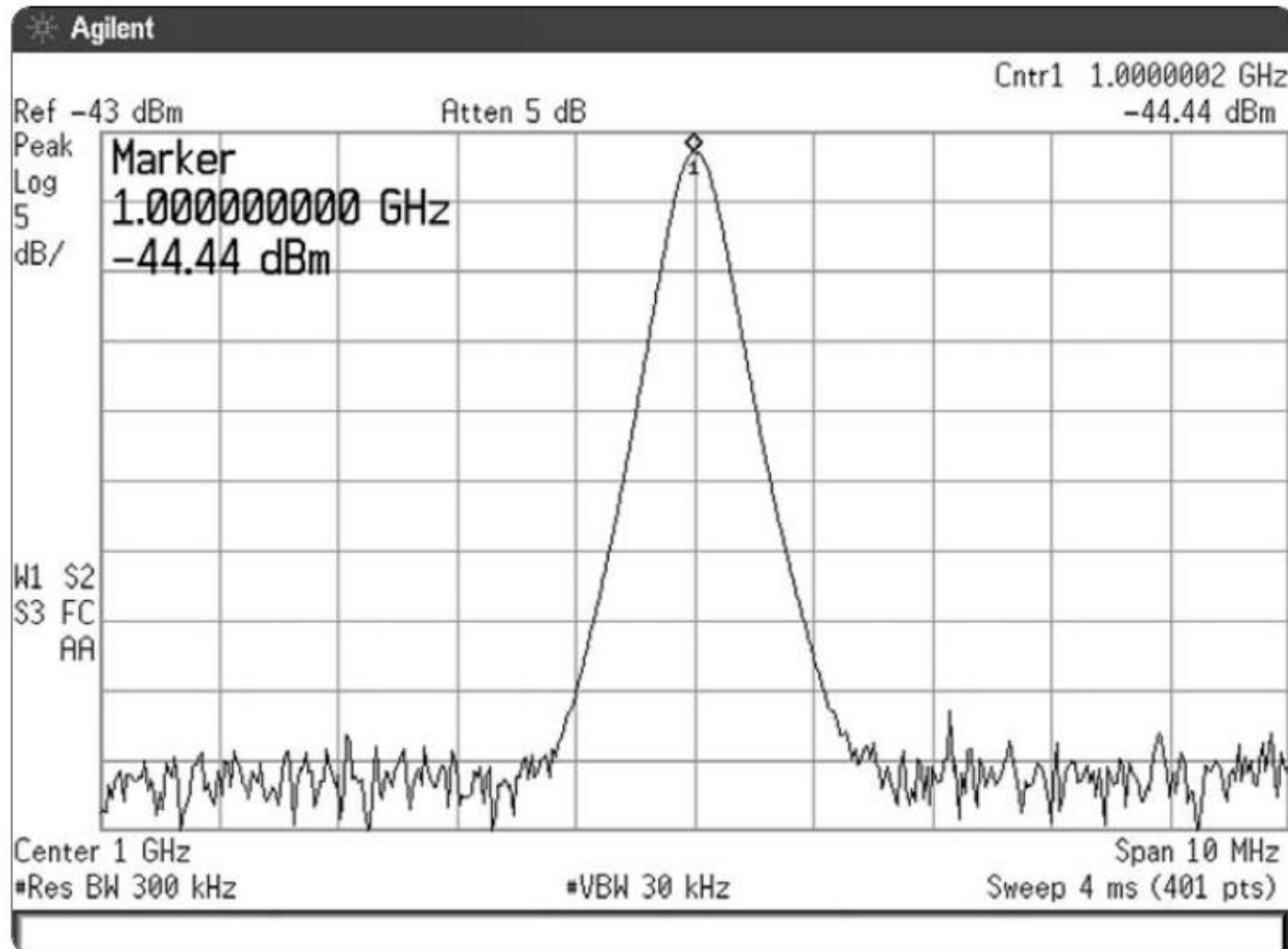


10 DIV vertical: POWER [dBm]

10 DIV horizontal: FREQUENCY [Hz]

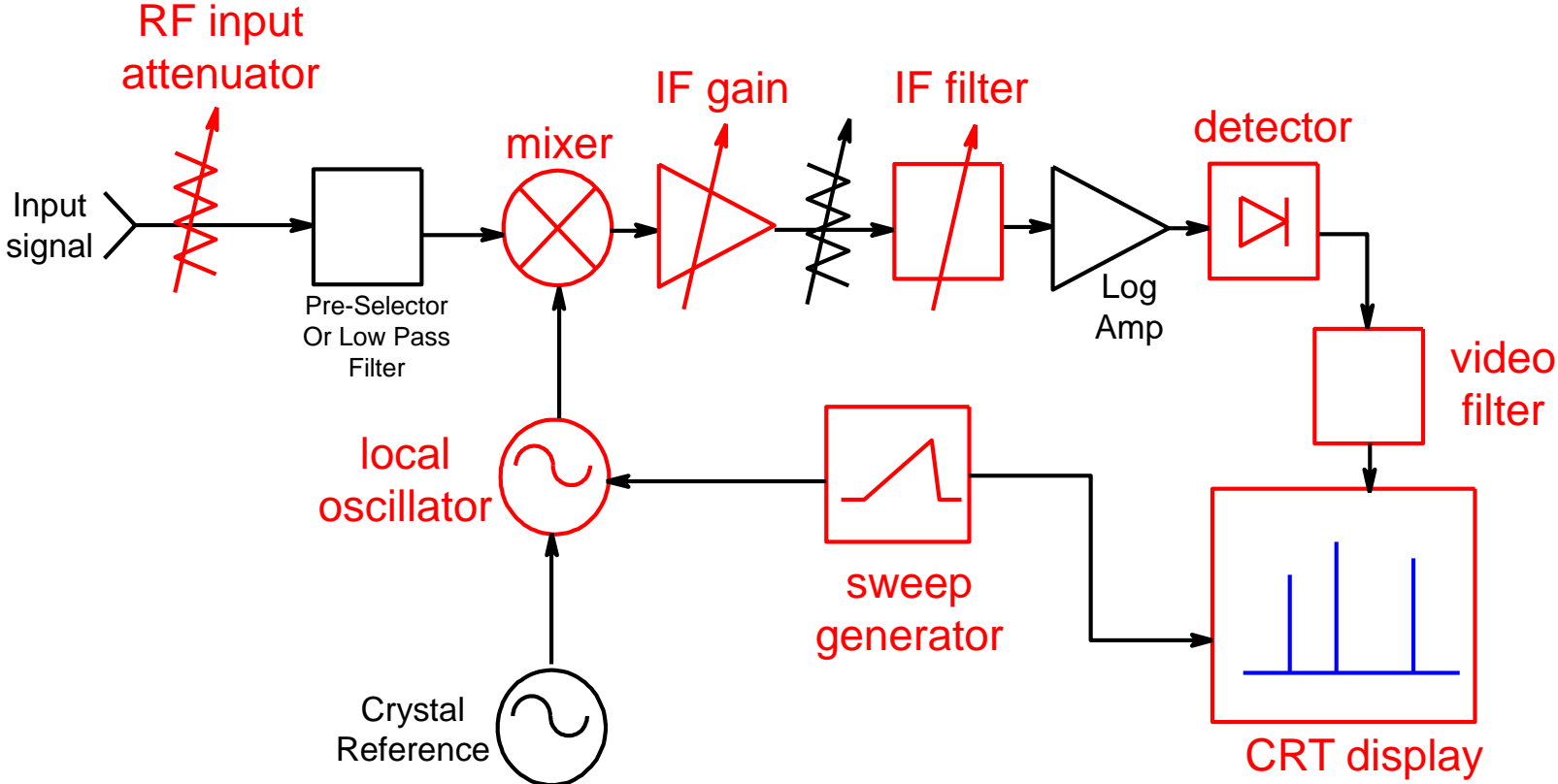


# Instrument Screen



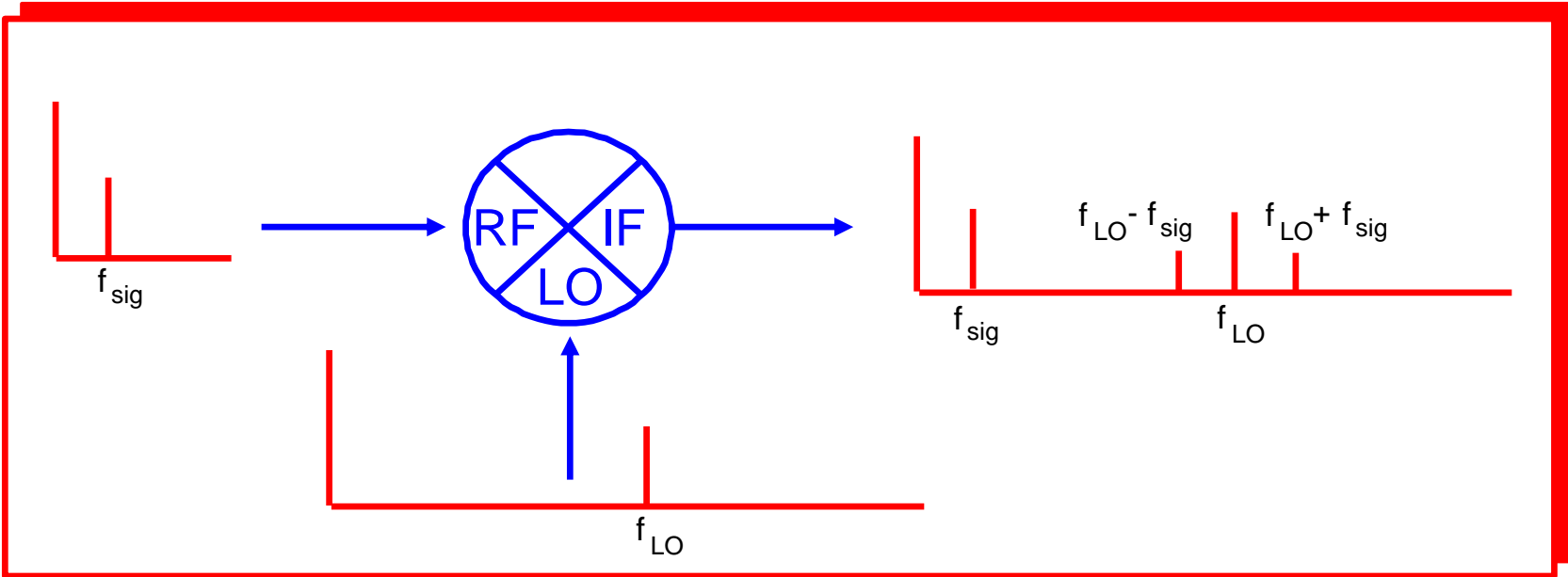
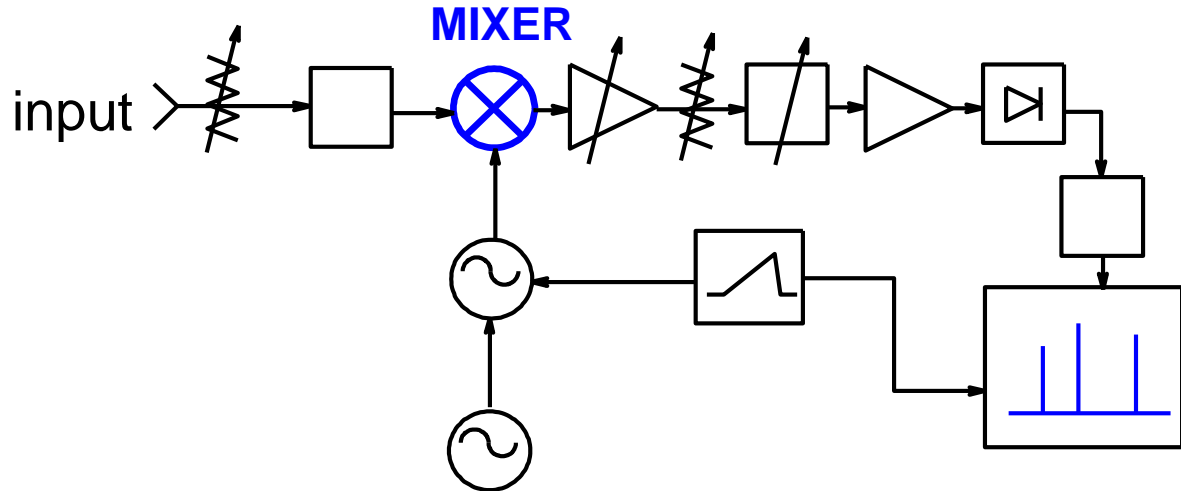
# Theory of Operation

## Spectrum Analyzer Block Diagram

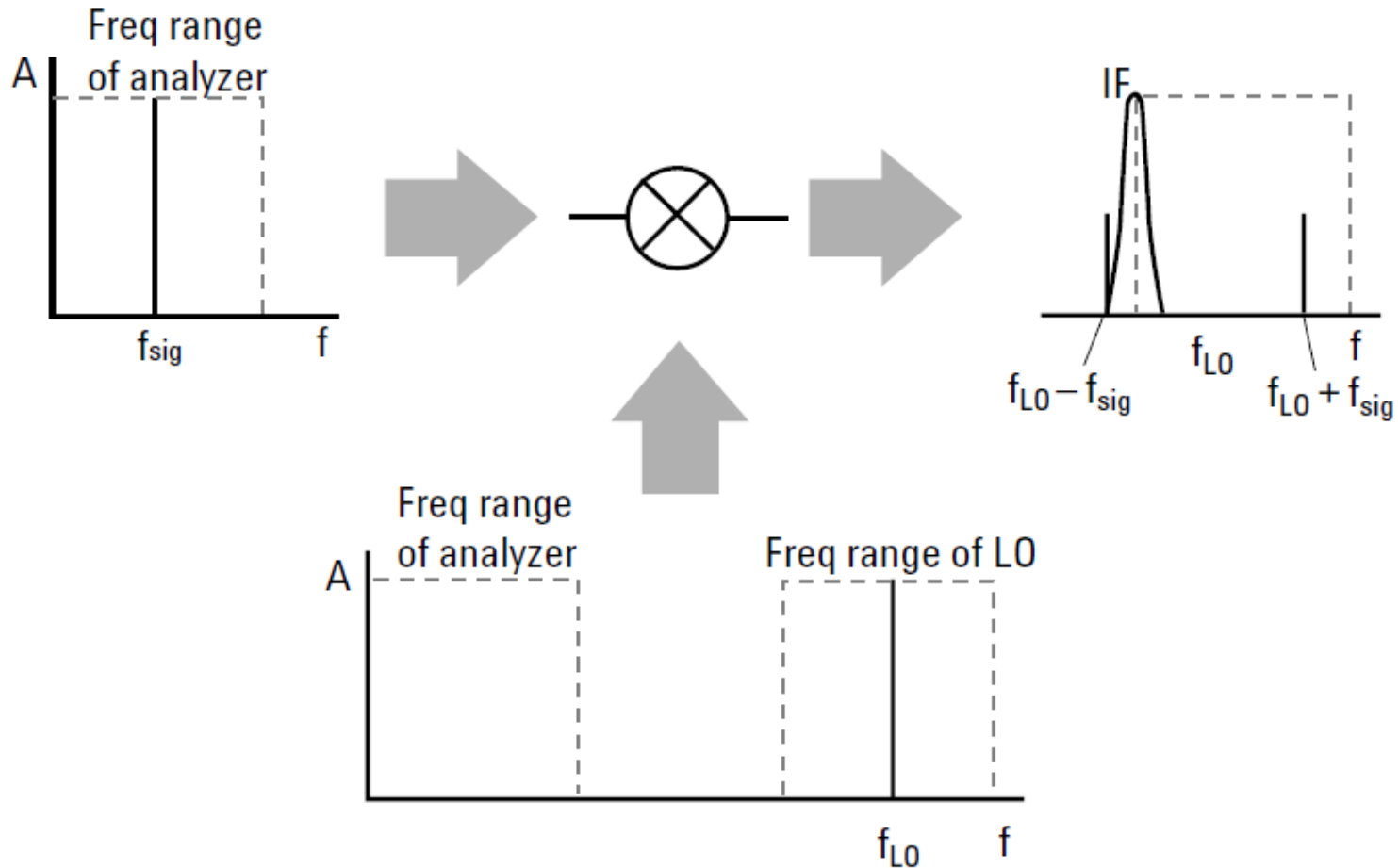


# Theory of Operation

## Mixer

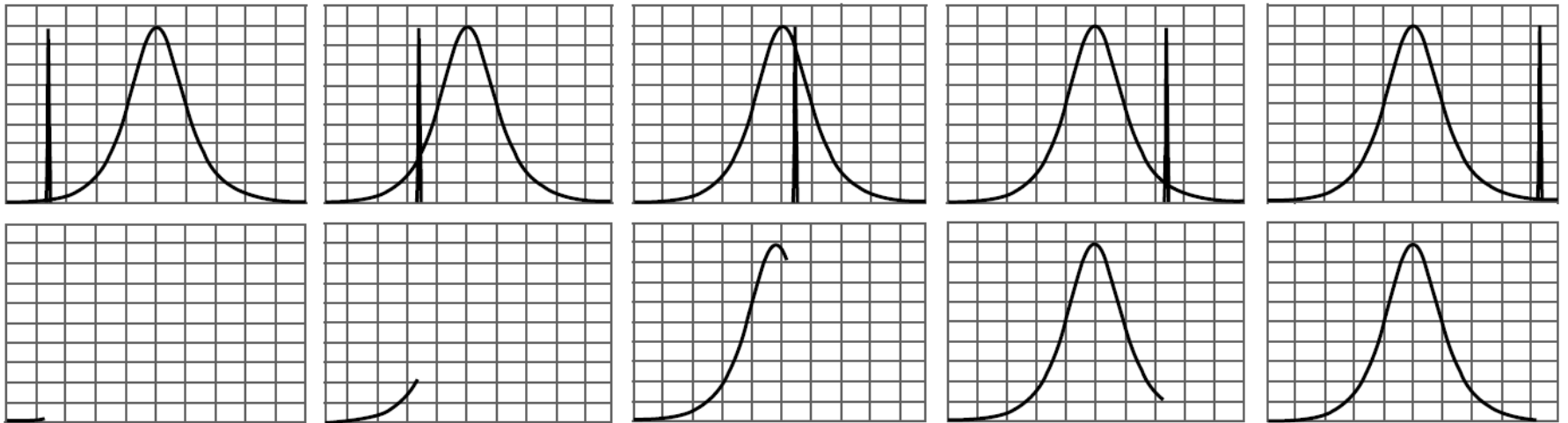


# Frequency Scan



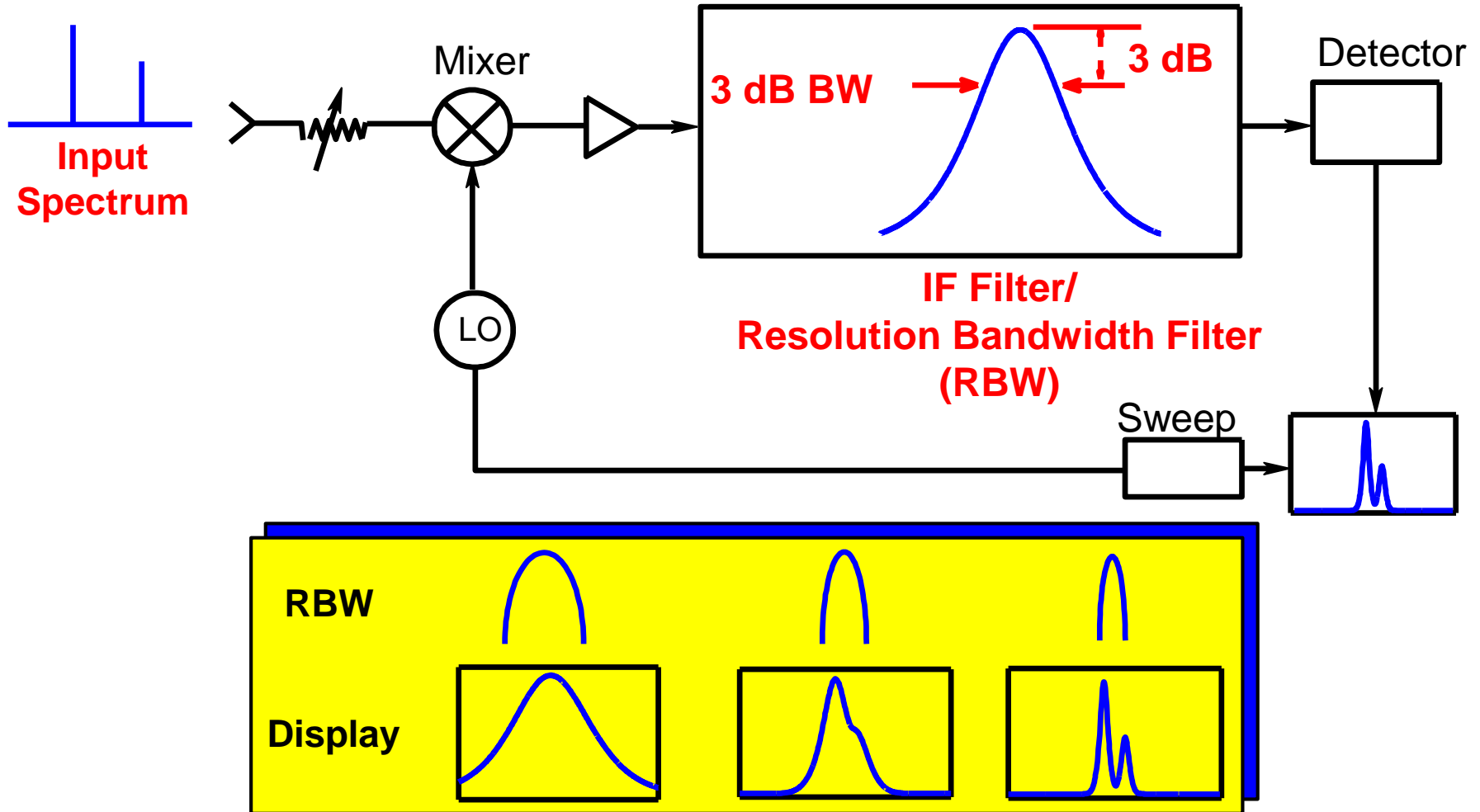
# Signal measurement

When a narrowband signal runs beneath the filter, the measured spectrum draws the filter shape (it is a mathematical convolution)



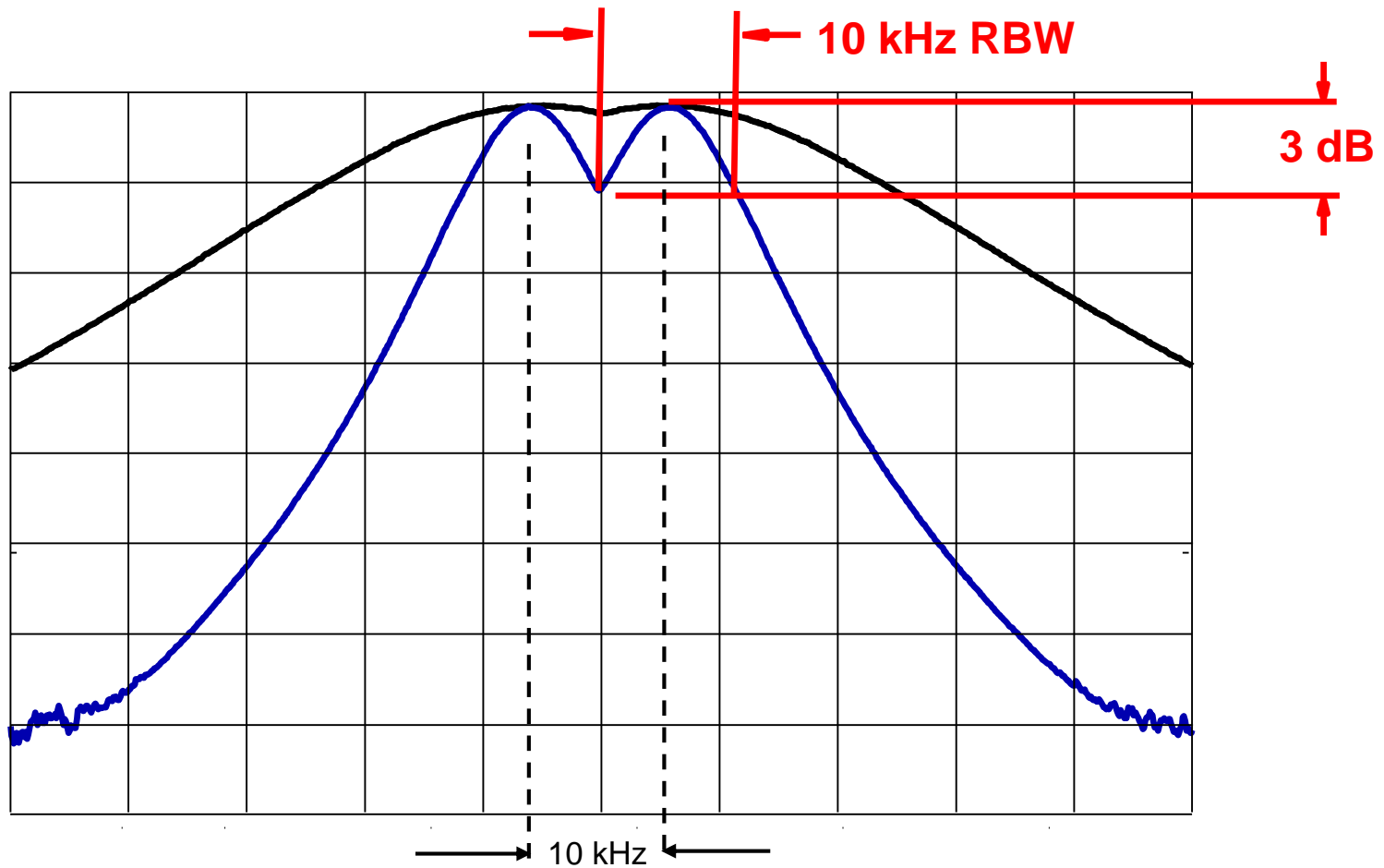
# Specifications

Resolution: Resolution Bandwidth

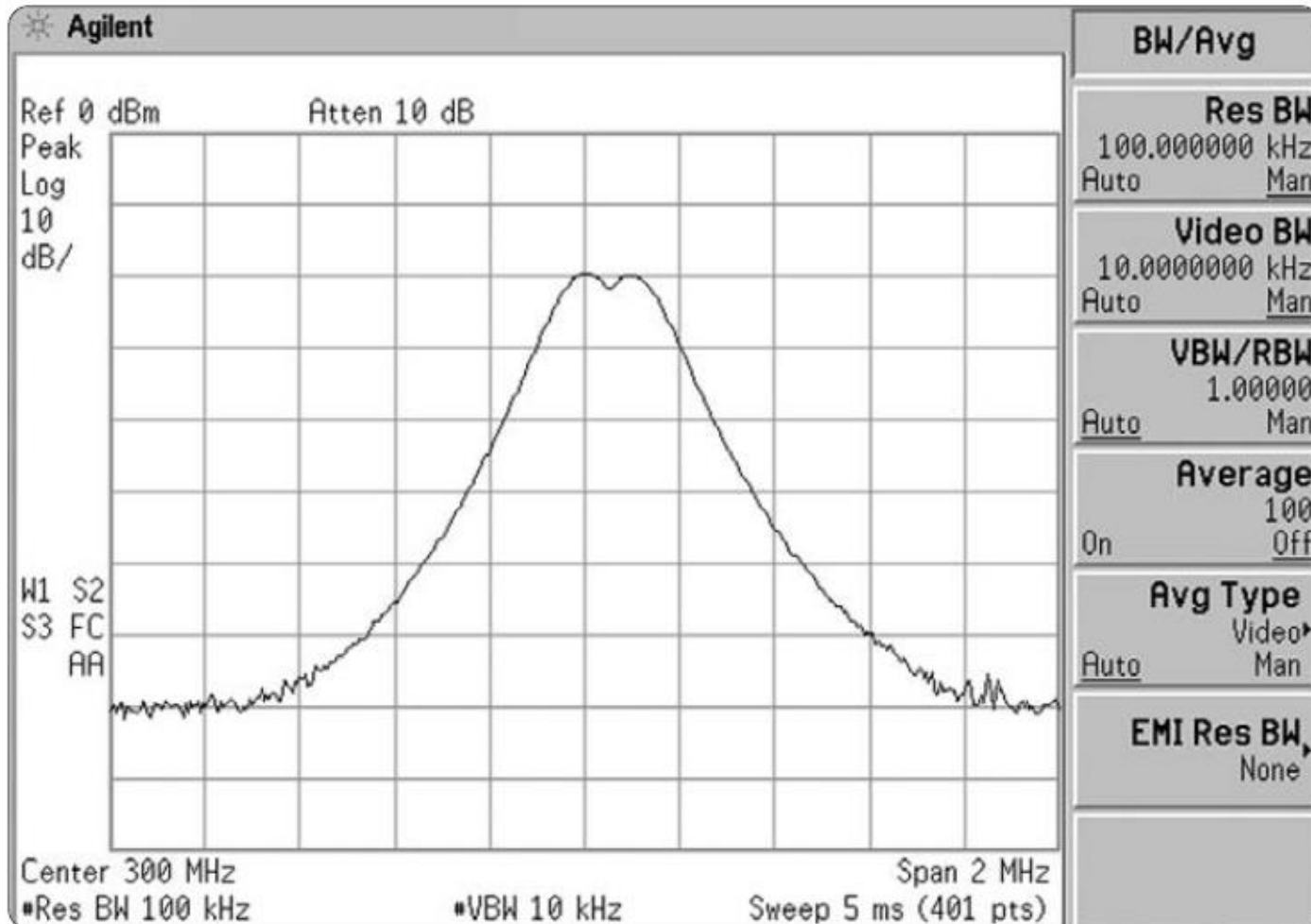


# Specifications

Resolution: Resolution Bandwidth



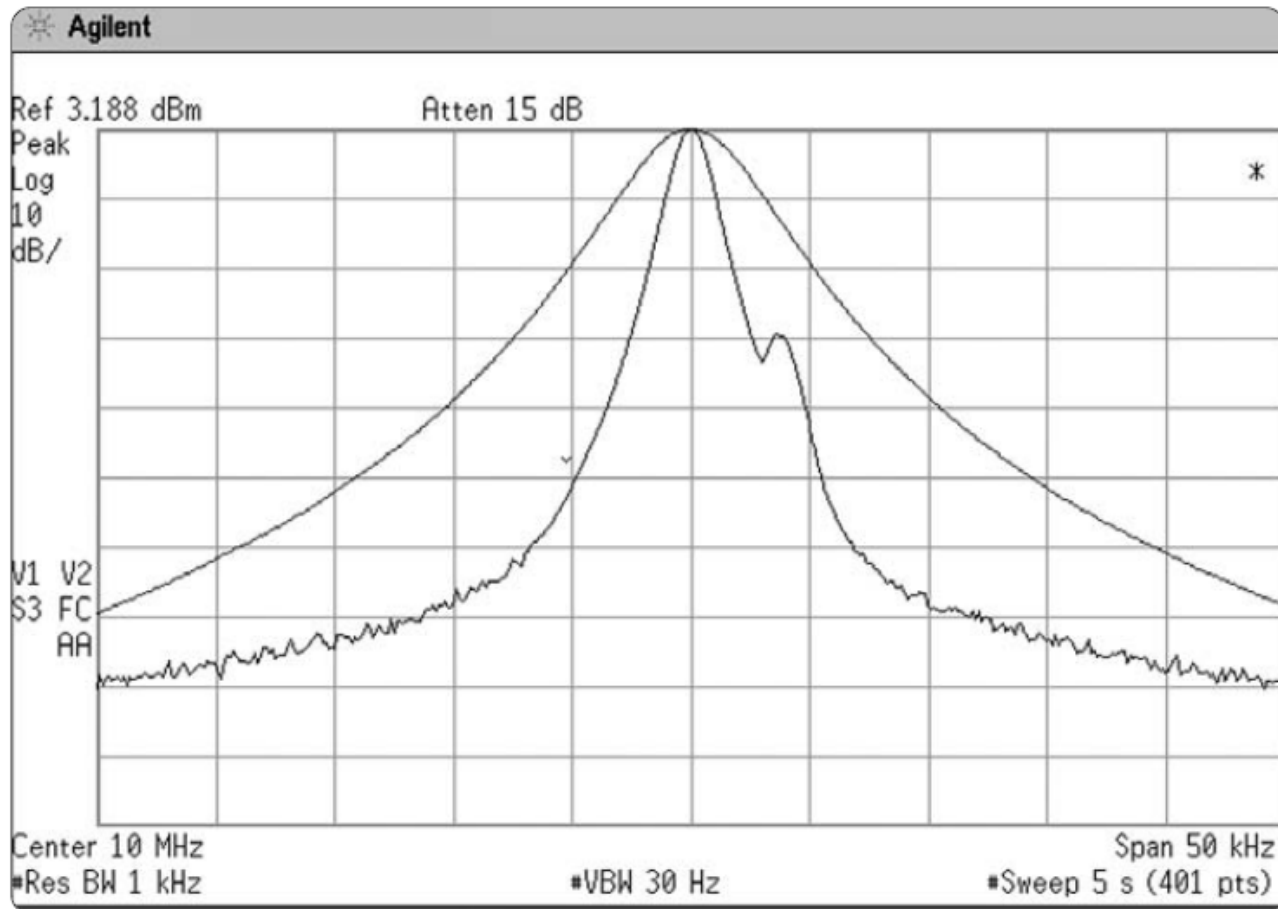
# Screen example



**Figure 2-7. Two equal-amplitude sinusoids separated by the 3 dB BW of the selected IF filter can be resolved**



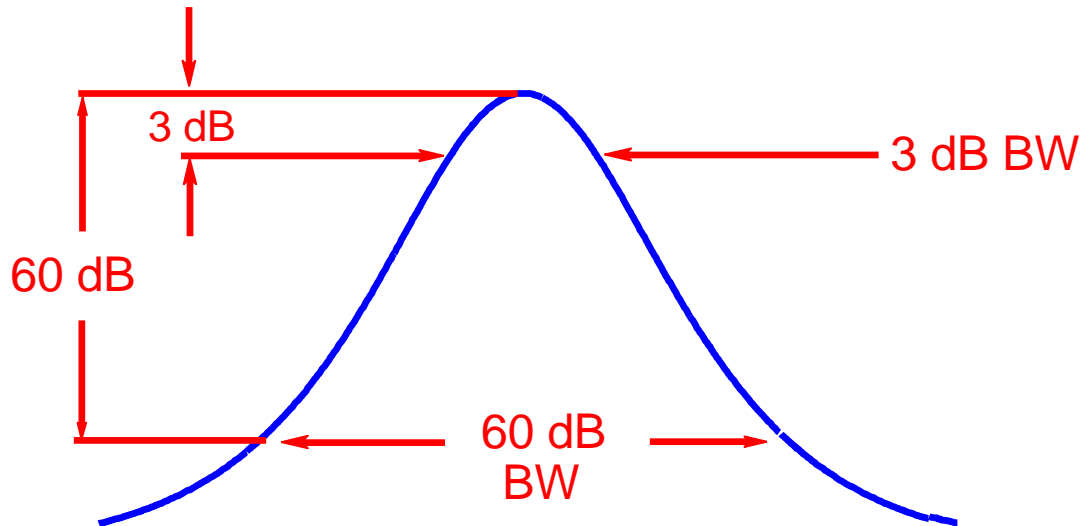
# Screen example



**Figure 2-10. The 3 kHz filter (top trace) does not resolve smaller signal; reducing the resolution bandwidth to 1 kHz (bottom trace) does**

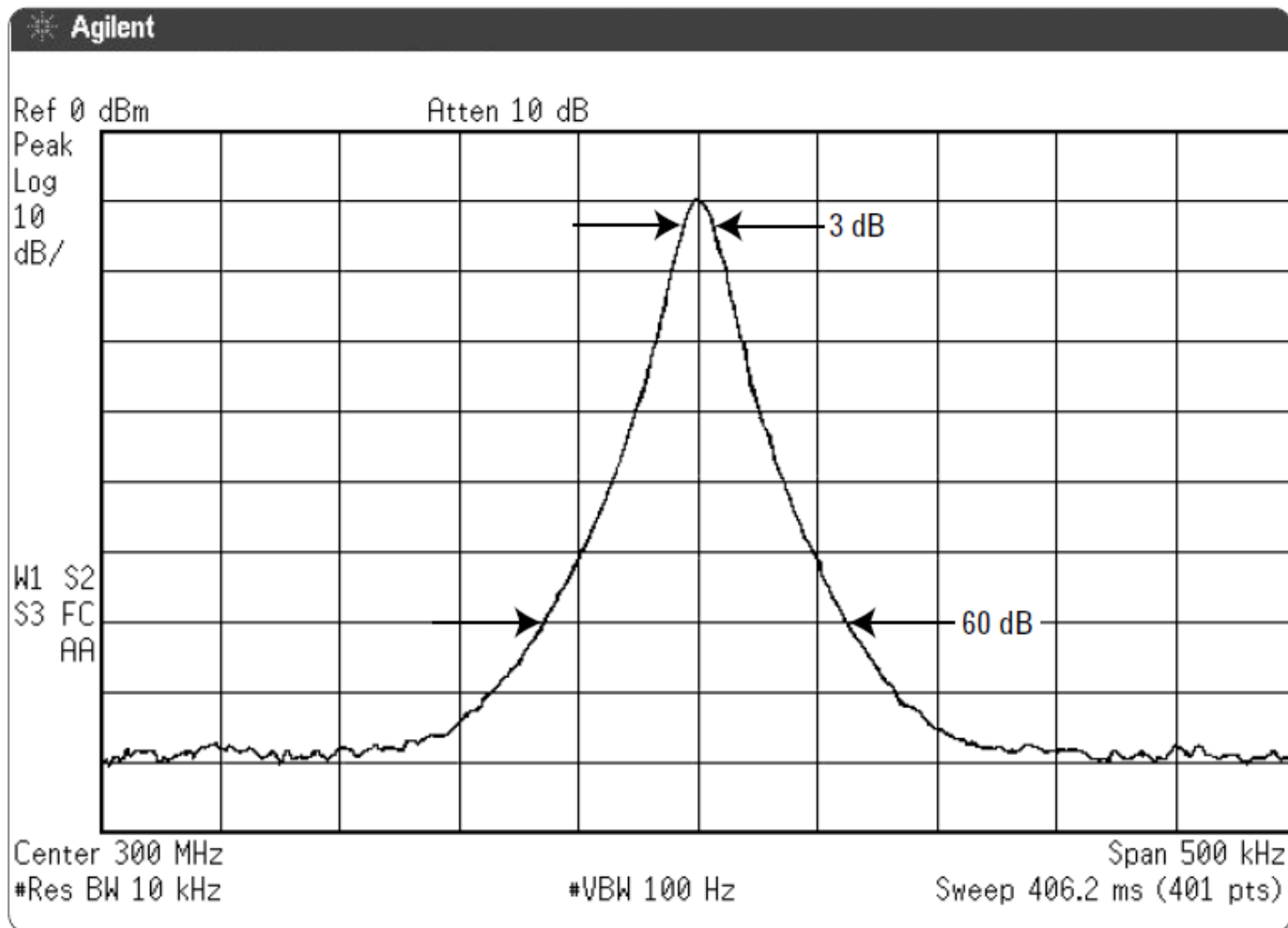
# Specifications

## Resolution: RBW Type and Selectivity



$$\text{Selectivity} = \frac{60 \text{ dB BW}}{3 \text{ dB BW}}$$

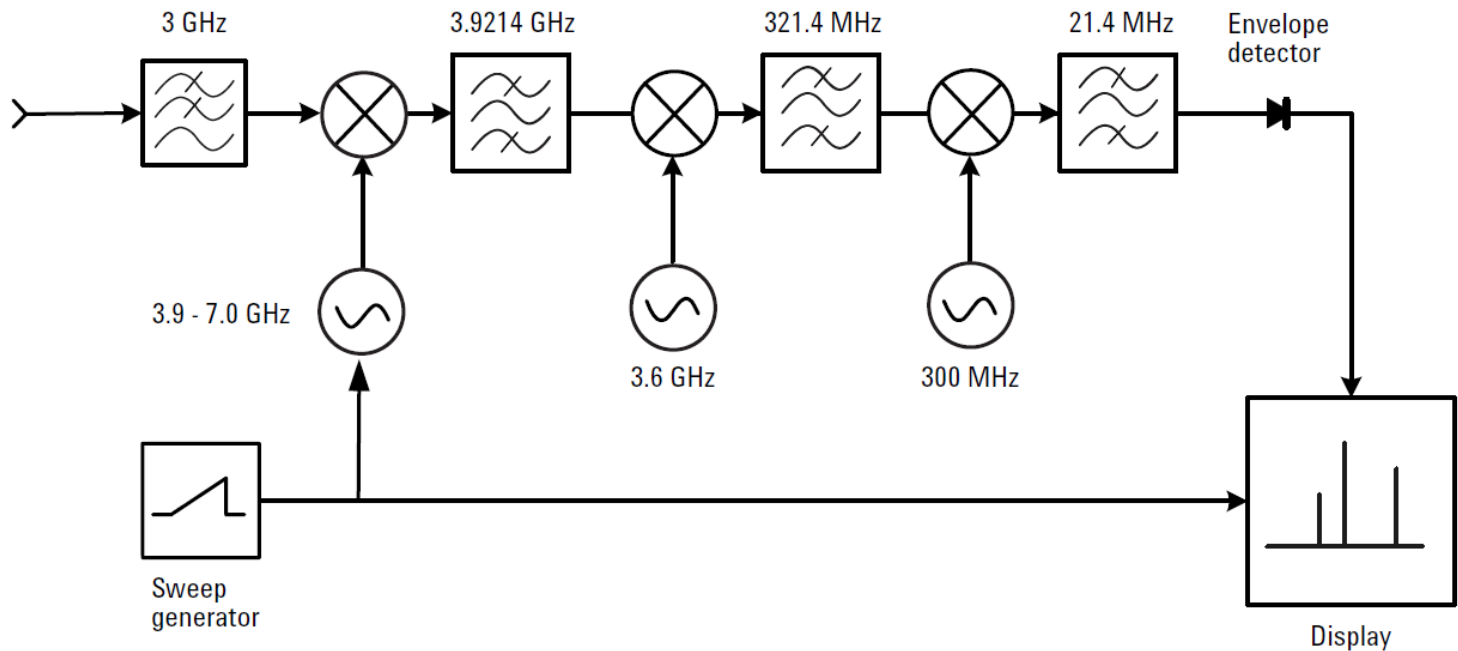
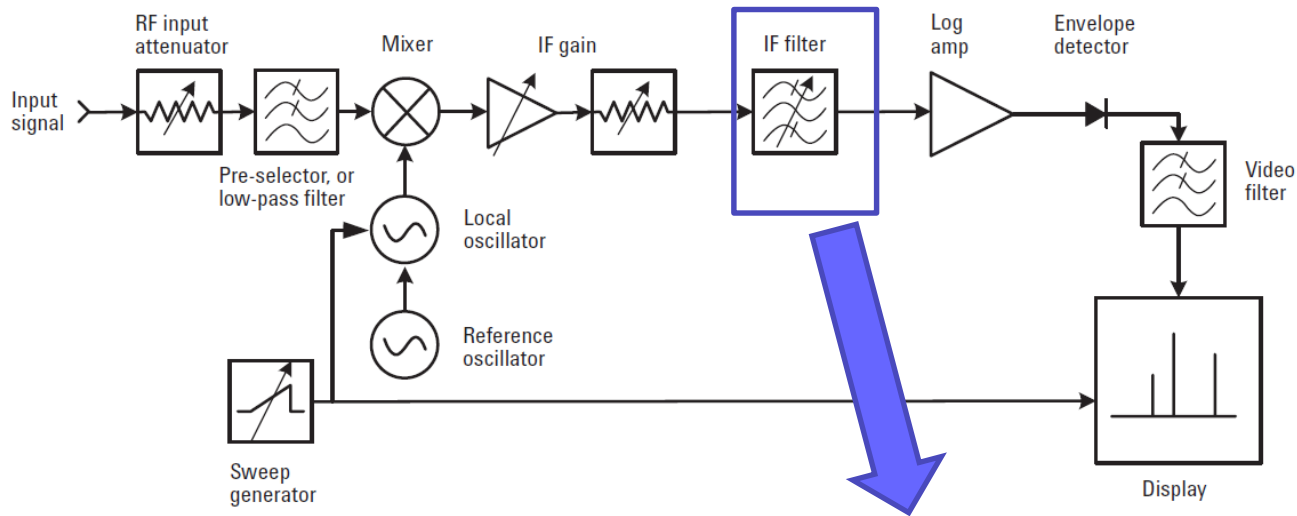
# Filter Selectivity



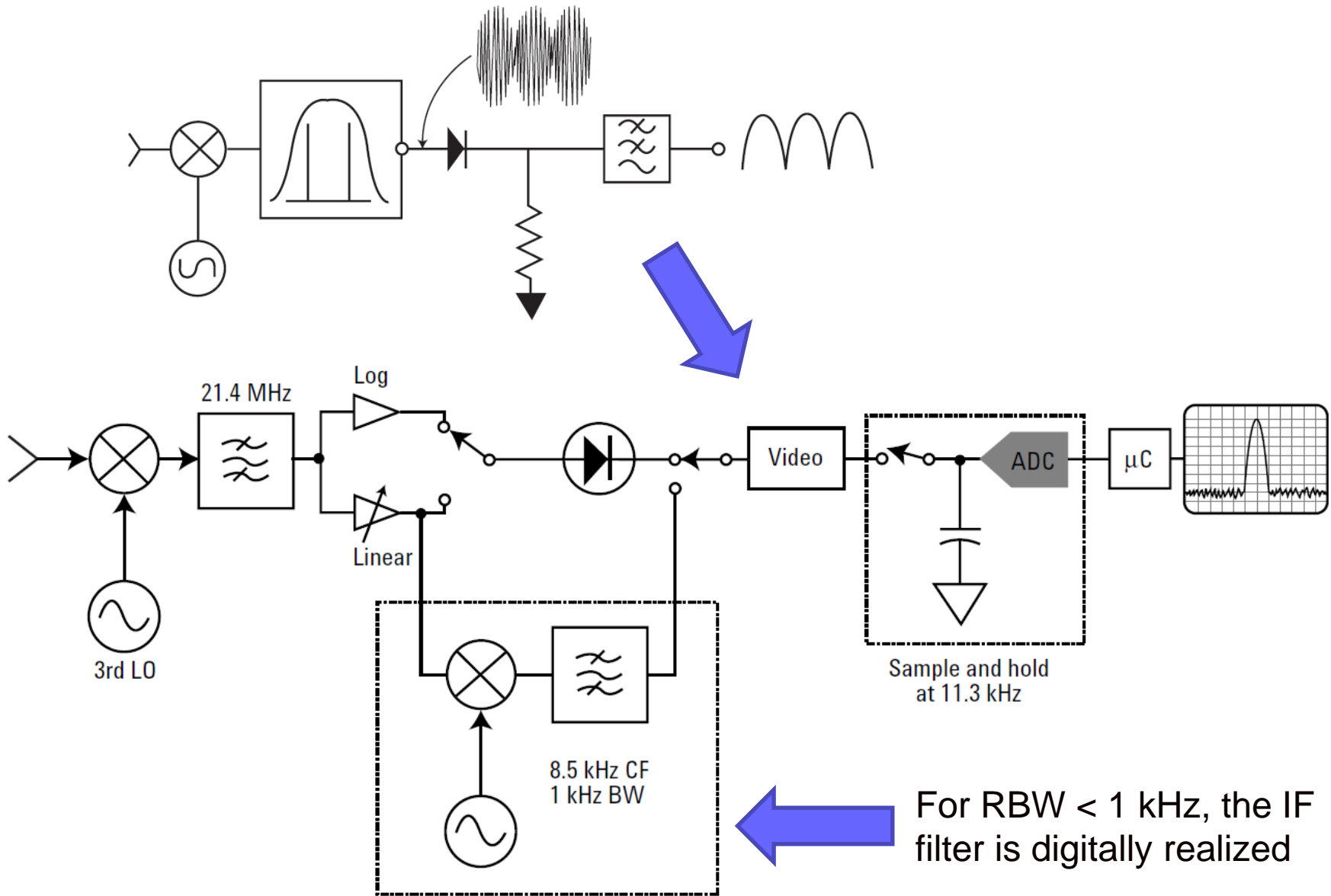
**Figure 2-9. Bandwidth selectivity, ratio of 60 dB to 3 dB bandwidths**



# Super-heterodyne detection

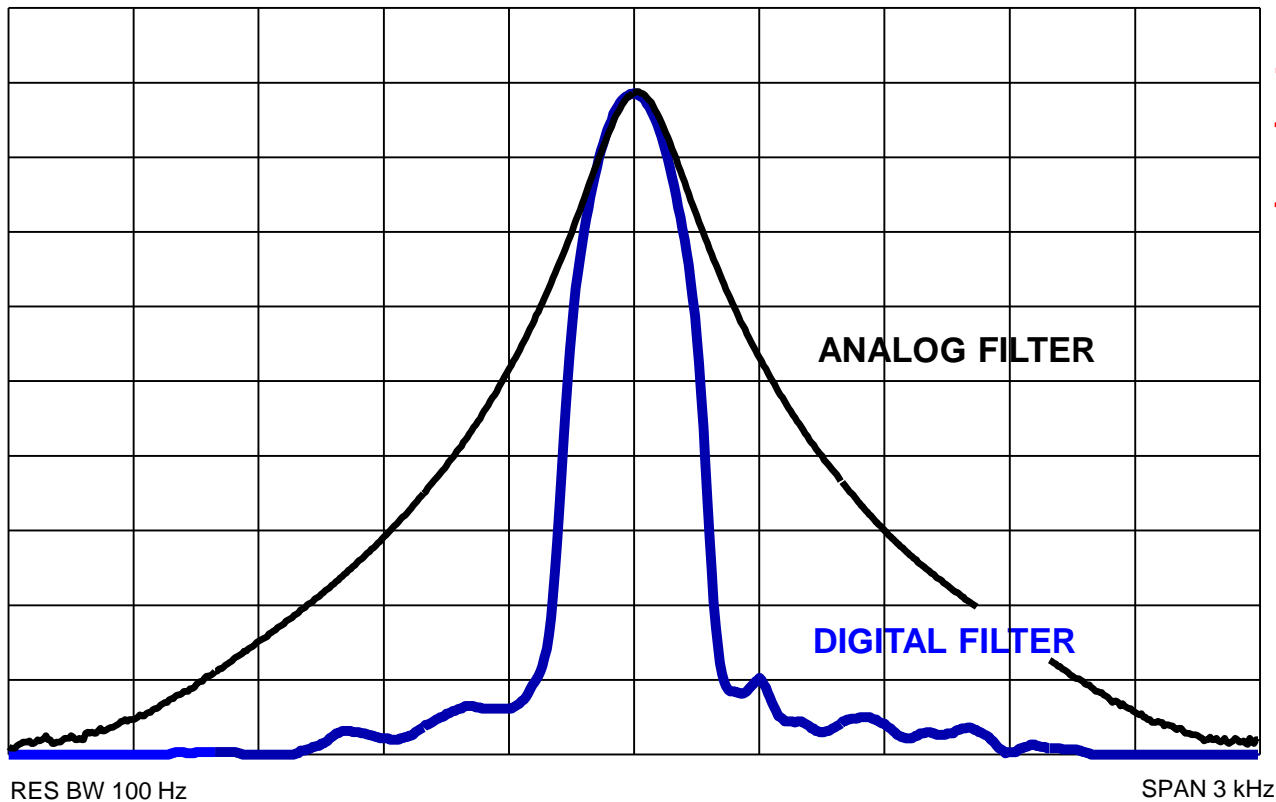


# Detector – from Analog to Digital



# Specifications

Resolution: Digital Resolution Bandwidths



Typical  
Selectivity

Analog

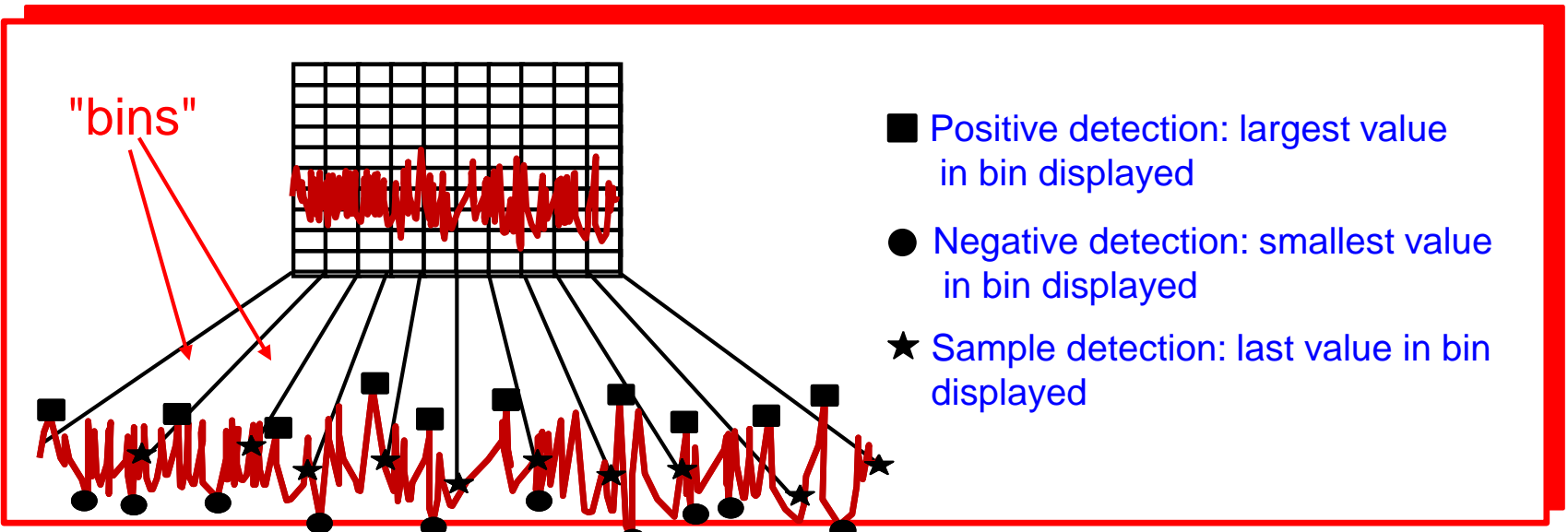
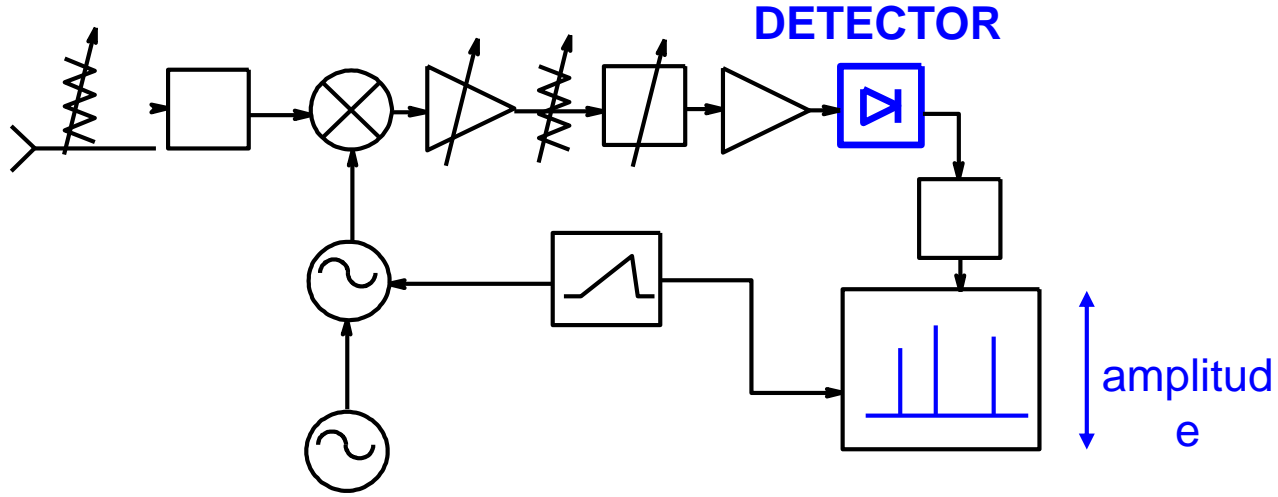
15:1

Digital

5:1

# Theory of Operation

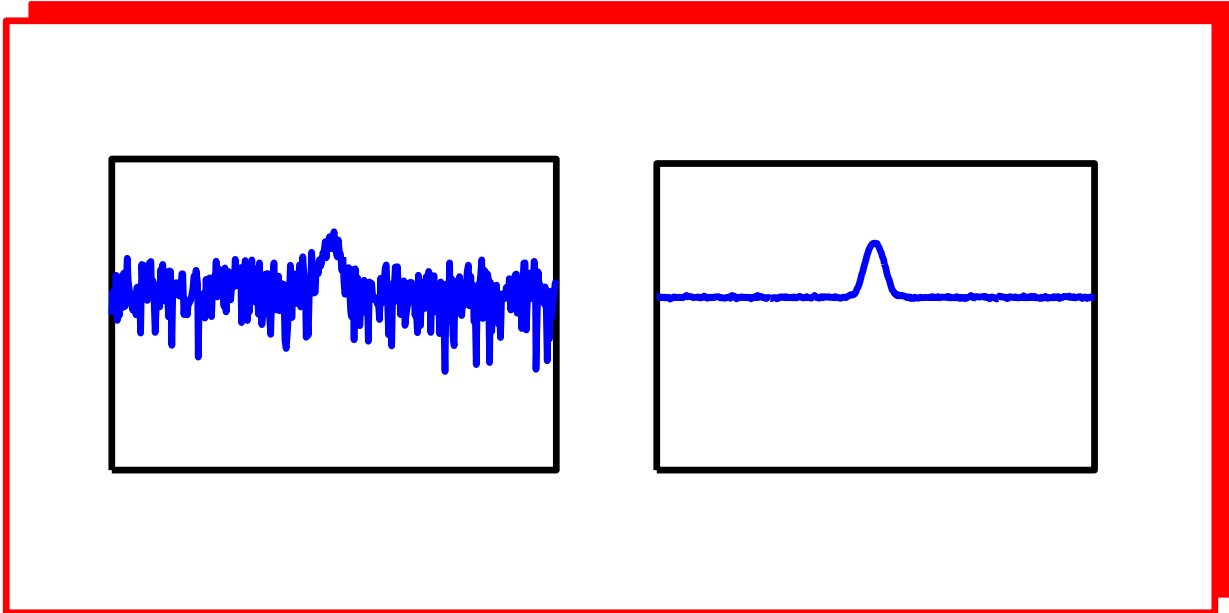
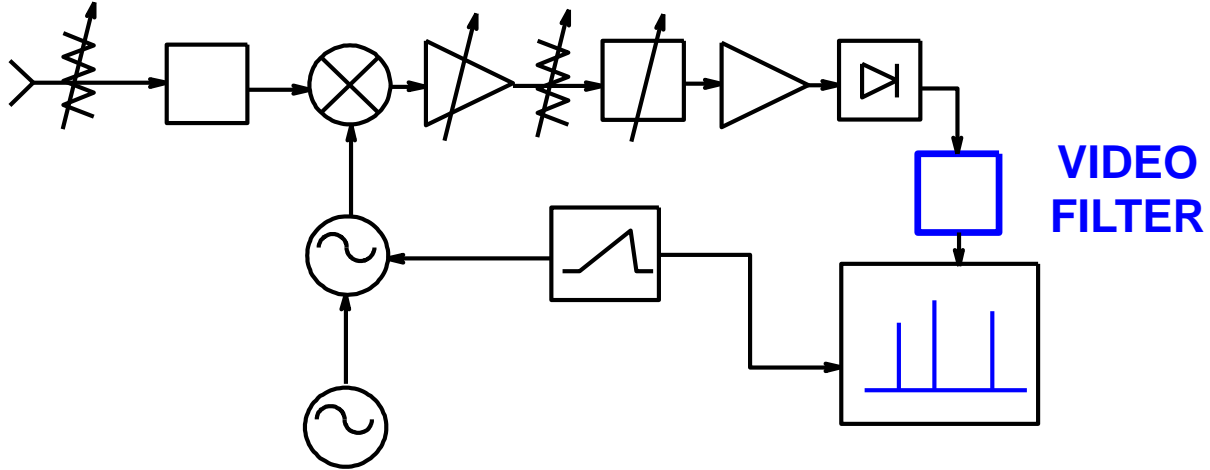
Detector





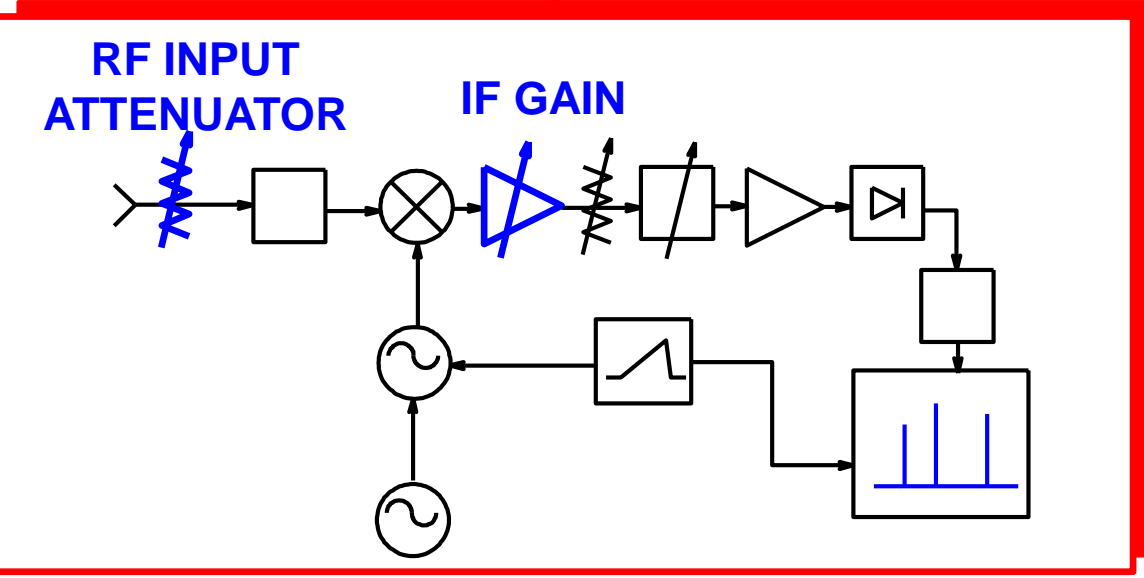
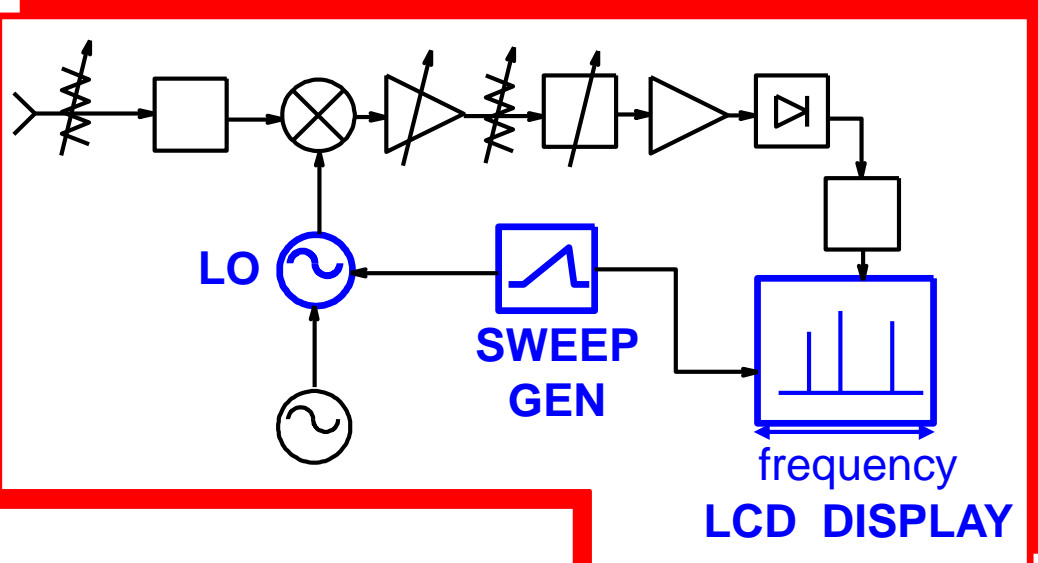
# Theory of Operation

## Video Filter



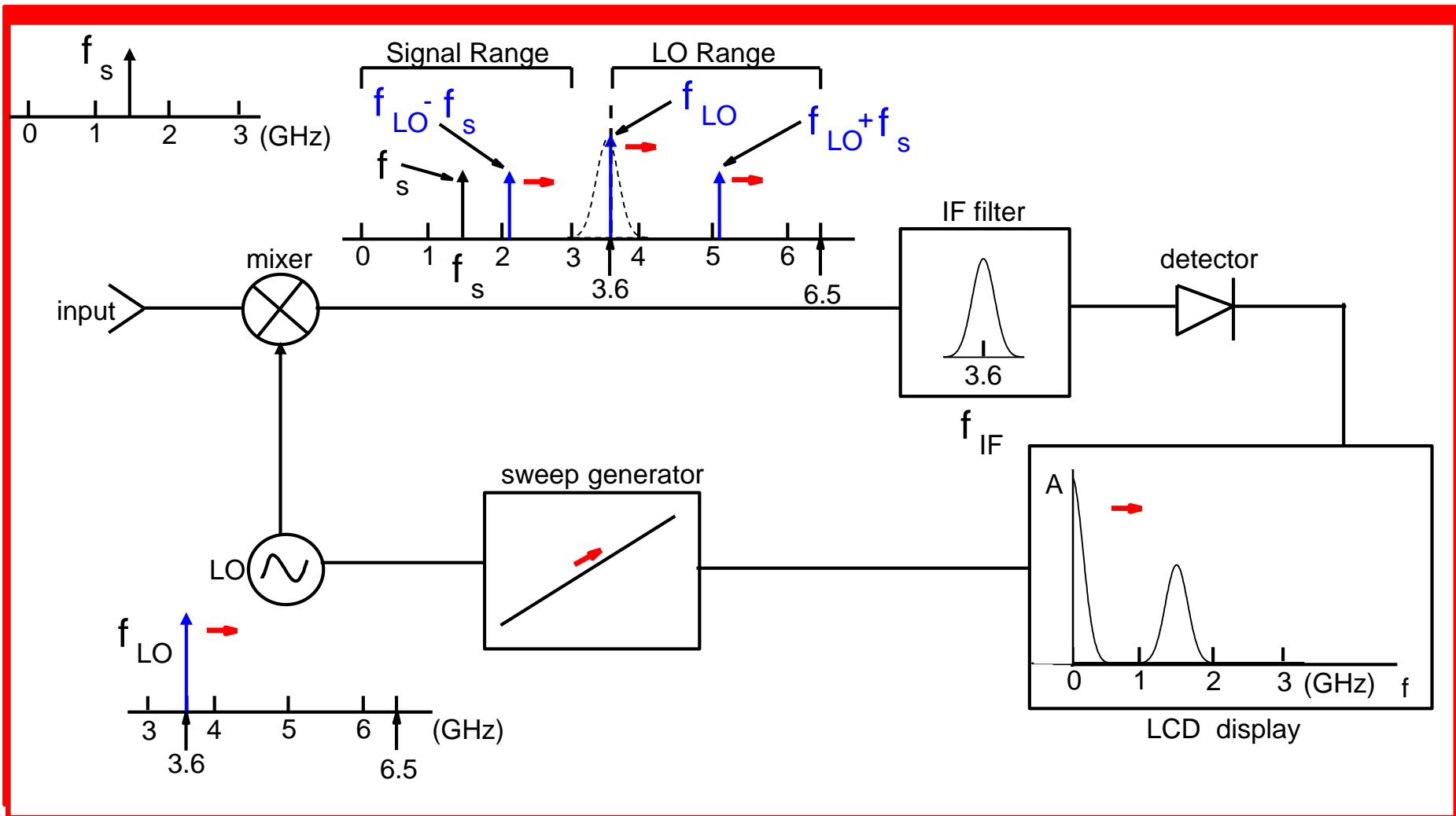
# Theory of Operation

## Other Components



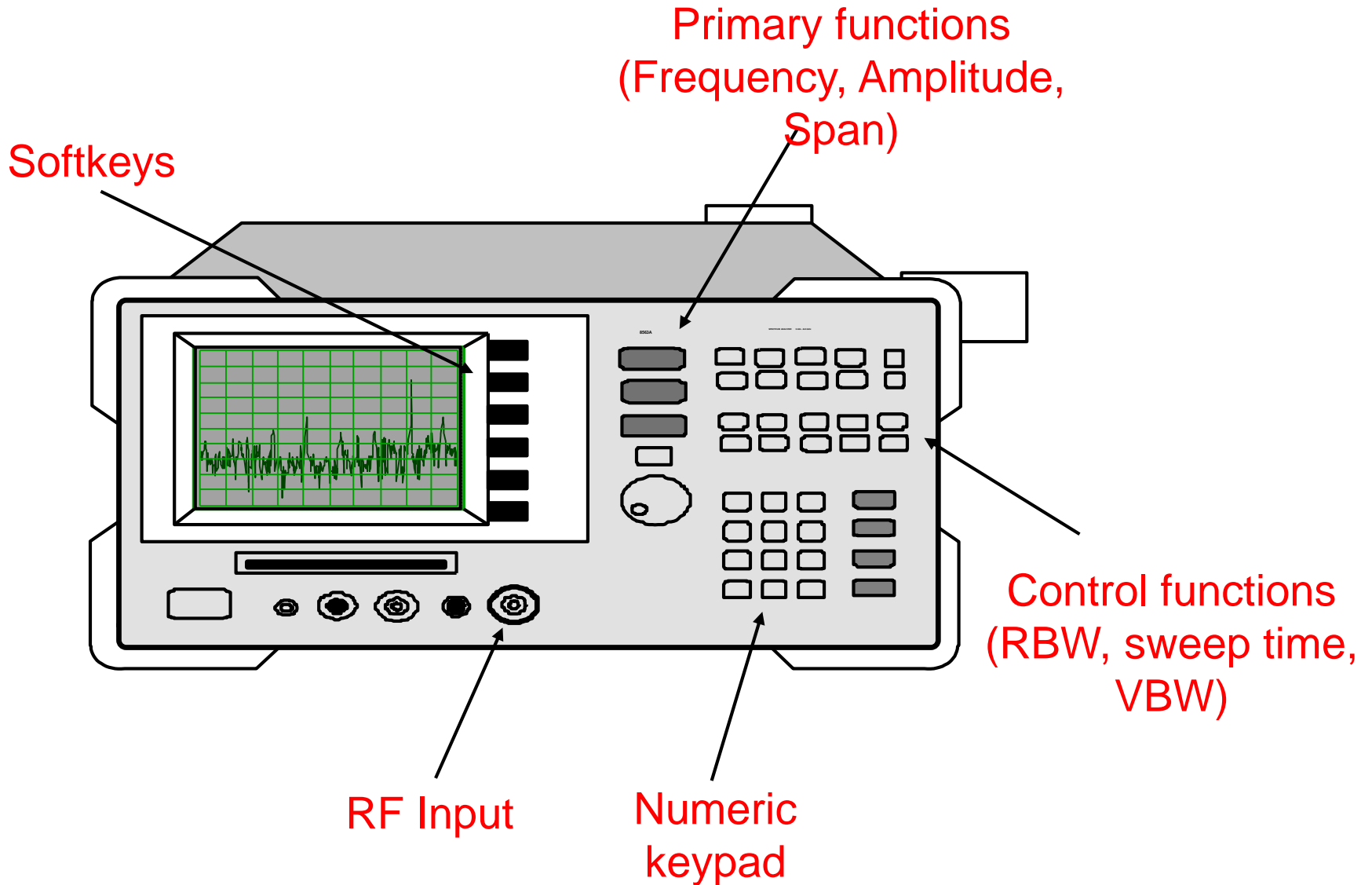
# Theory of Operation

How it all works together



# Theory of Operation

## Front Panel Operation



# Swept Spectrum Analyzer: Measurement Time

The rise time of a filter (low-pass, but also band-pass) is inversely proportional to its bandwidth, and if we include a constant of proportionality,  $k$ , then:

$$\text{Rise time} = T = k / RBW$$

The value of  $k$  is in the 2 to 3 range for the synchronously-tuned, near-Gaussian filters used in many analyzers.

The number  $N$  of “equivalent points” on a screen is given by

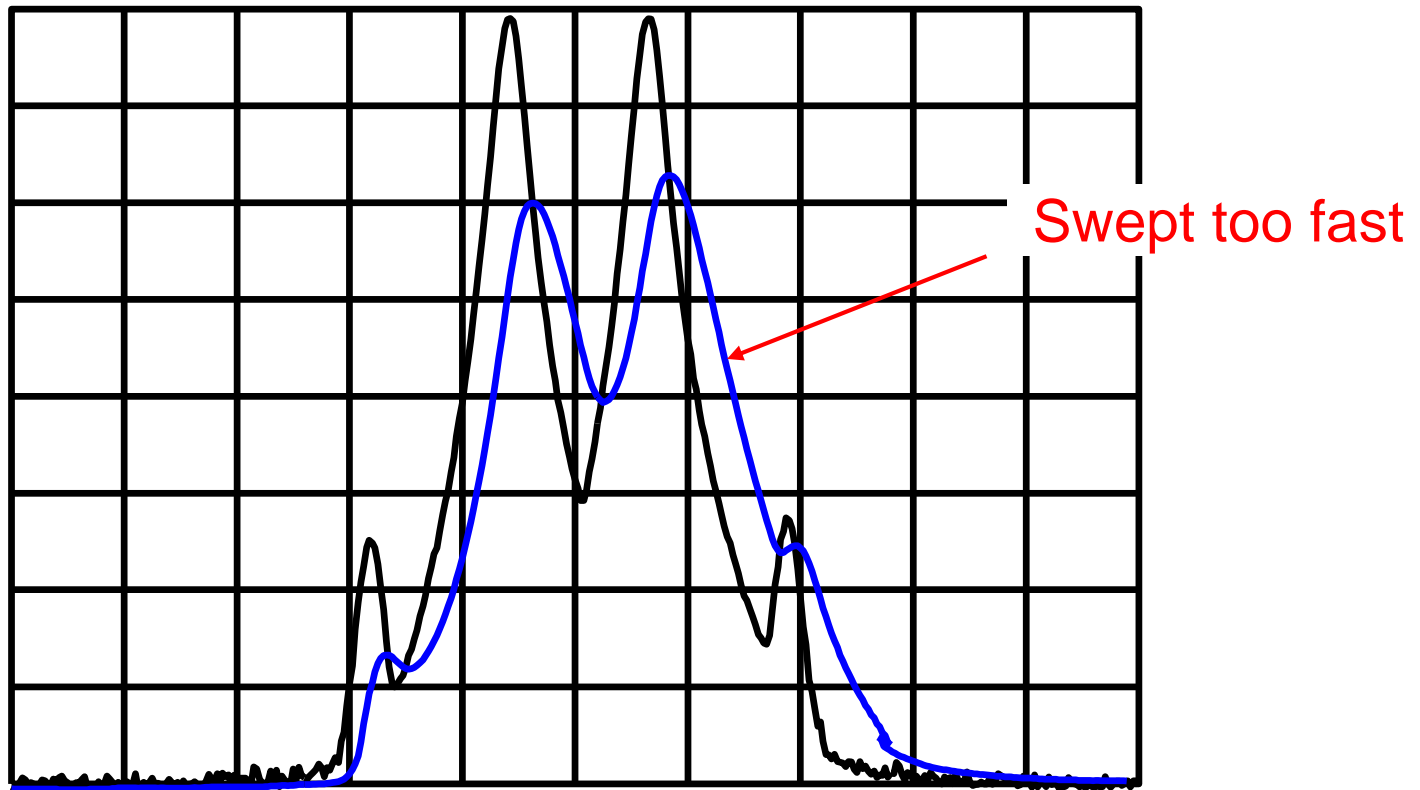
$$N = \text{Span} / RBW$$

In conclusion, the minimum sweep time for a correct measurement is

$$ST = N \times T \approx \frac{3\text{Span}}{RBW^2}$$

# Specifications

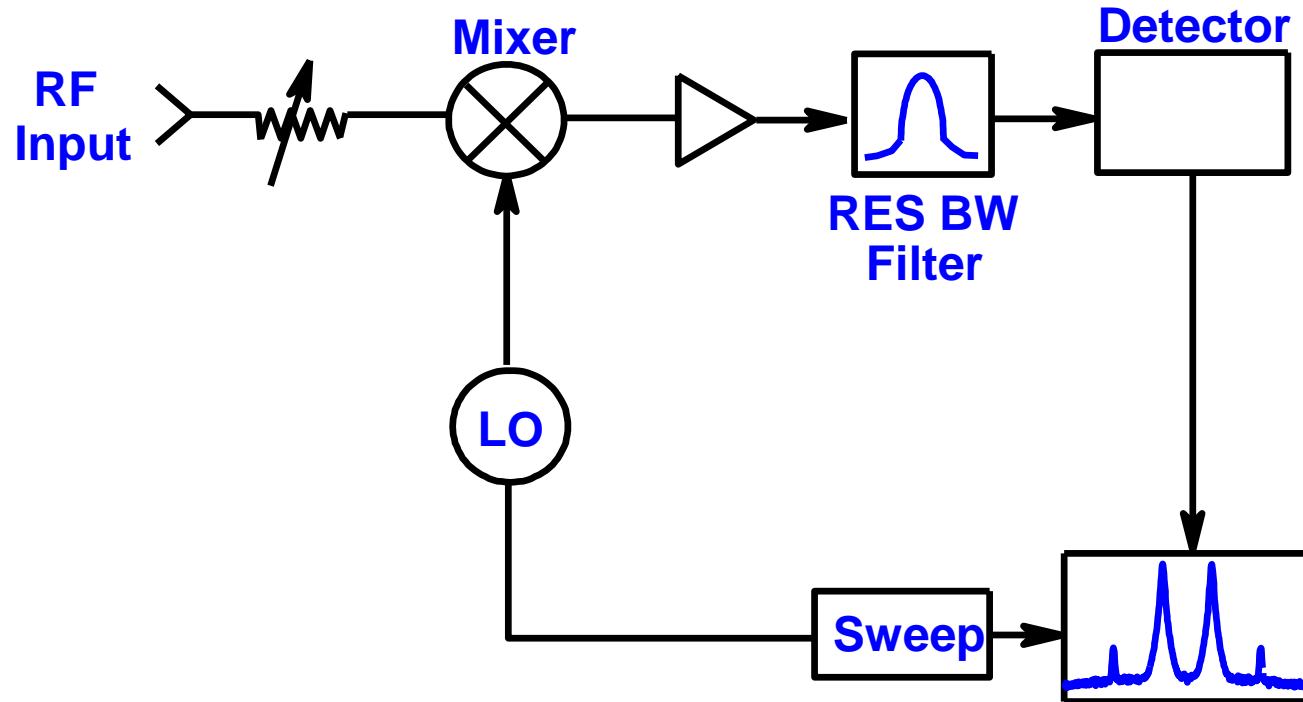
Resolution: RBW Determines Measurement Time



**Penalty For Sweeping Too Fast  
Is An Uncalibrated Display**

# Specifications

Sensitivity/DANL

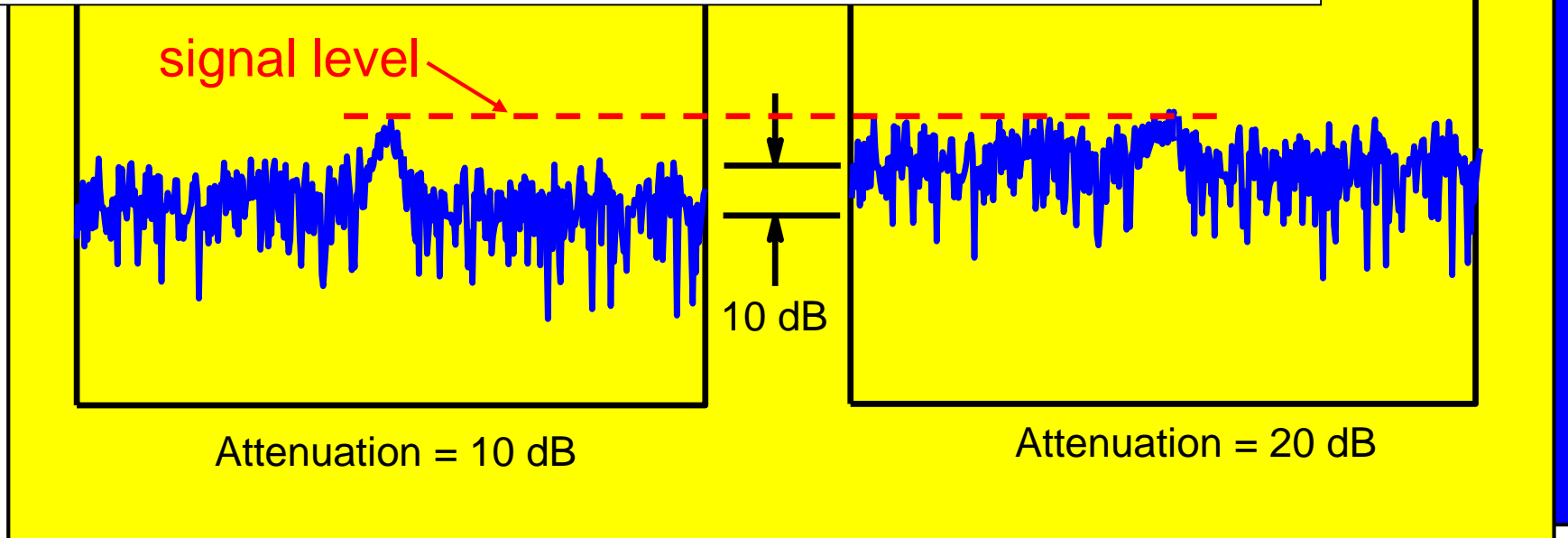


**A Spectrum Analyzer Generates and Amplifies Noise Just Like Any Active Circuit**

# Specifications

## Sensitivity/DANL

Effective Level of Displayed Noise is a Function of RF Input Attenuation



Signal-To-Noise Ratio Decreases as RF Input Attenuation is Increased



# Attenuation - Noise Level (DANL)

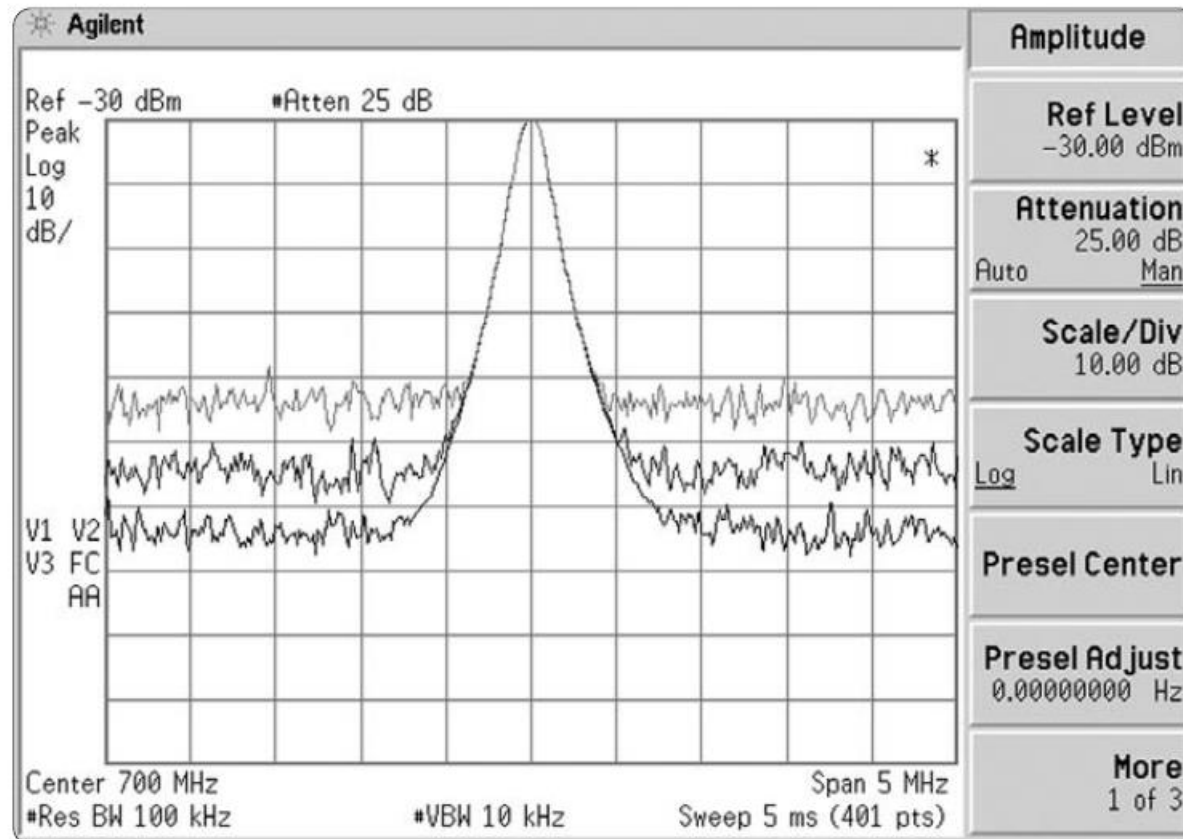


Figure 5-1. Reference level remains constant when changing input attenuation

# Noise Figure and DANL

The spectral density of thermal noise is equal to:

$$p_T = kT \cong 4 \times 10^{-21} \text{ W/Hz} \cong -174 \text{ dBm/Hz}$$

At ambient temperature, and  $k = 1.38 \times 10^{-23} \left[ \frac{\text{W}}{\text{Hz K}} = \frac{\text{J}}{\text{K}} \right]$  is the Boltzmann constant

Noise Figure is defined as the ratio between the instrument noise level and the thermal noise:

$$\begin{aligned} NF &= DANL[\text{measured noise in dBm}] - 10 \log[kT \times RBW/(1 \text{ mW})] = \\ &= DANL[\text{measured noise in dBm}] - 10 \log(RBW/1 \text{ Hz}) - (-174 \text{ dBm/Hz}) \\ &\quad (\text{in the approximation of equivalent-noise-bandwidth} \cong RBW) \end{aligned}$$

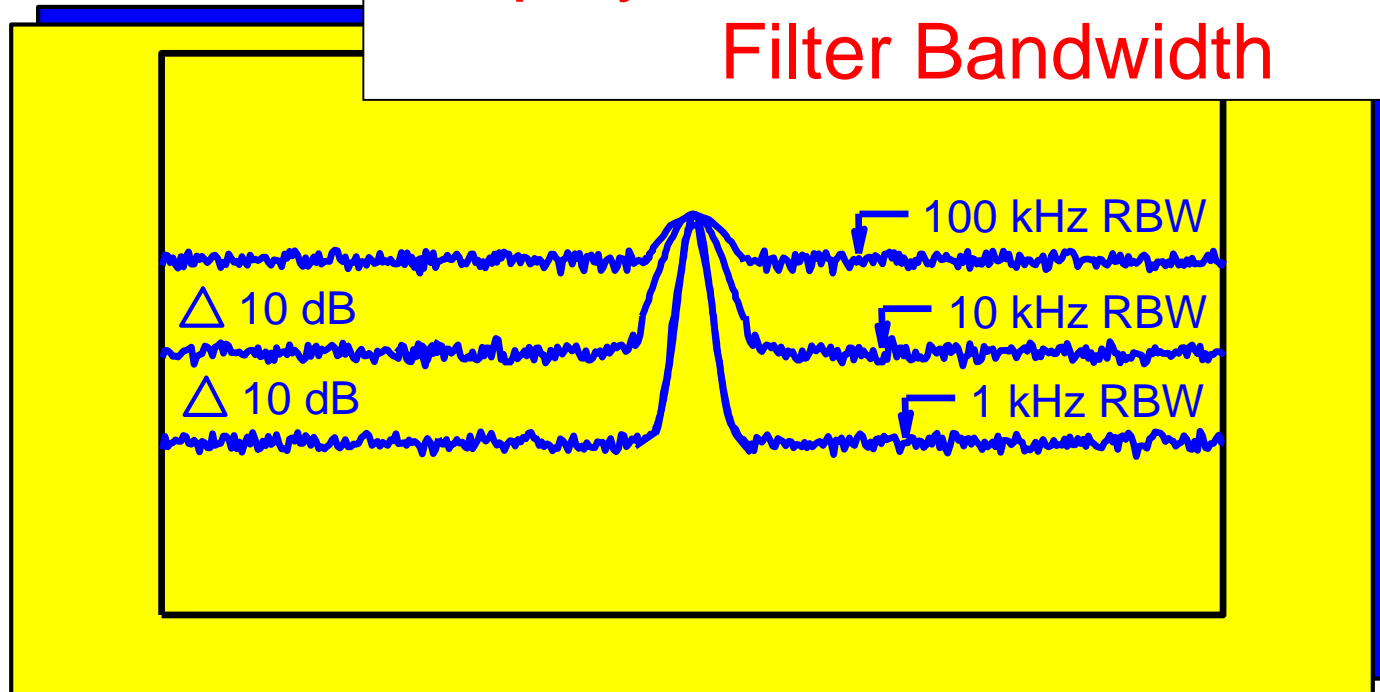
Noise figure is independent of IF-filter bandwidth, while the displayed averaged noise level (DANL) on the analyzer changes with bandwidth.

A typical value for  $NF$  is 20-24 dB

# Specifications

Sensitivity/DANL: IF Filter (RBW)

Displayed Noise is a Function of IF Filter Bandwidth



Decreased BW = Decreased Noise

# RBW – Noise Level (DANL)

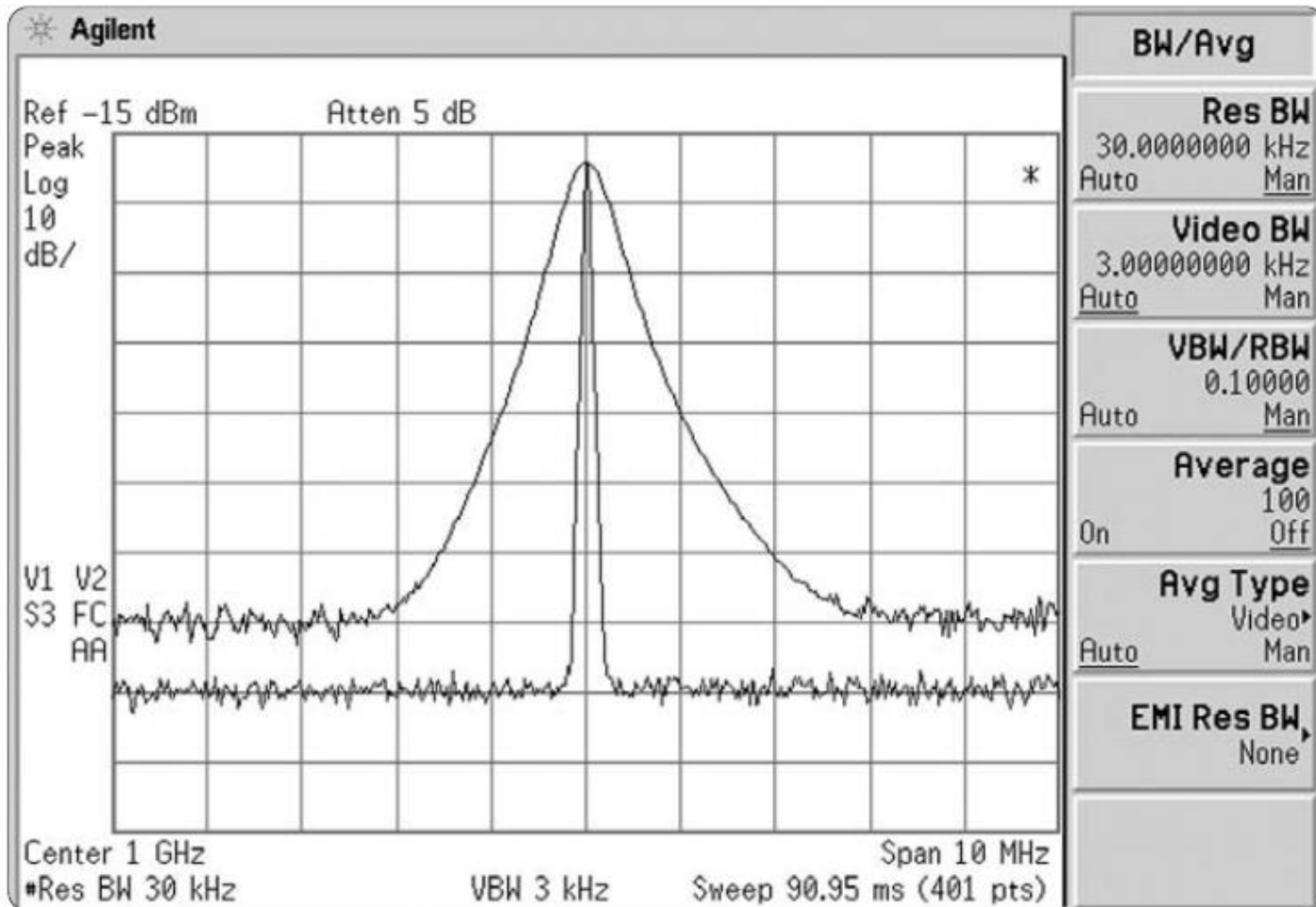
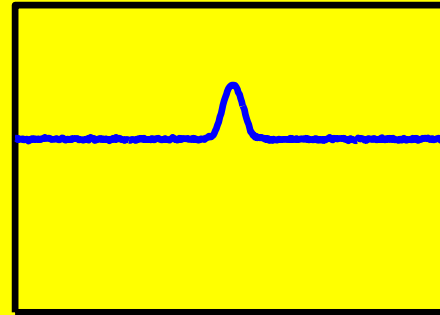
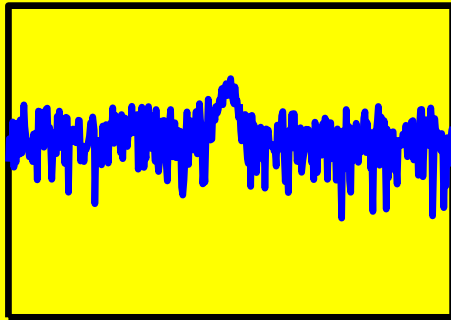


Figure 5-2. Displayed noise level changes as  $10 \log(BW_2/BW_1)$

# Specifications

Sensitivity/DANL: VBW

Video BW Smooths Noise for Easier Identification of Low Level Signals

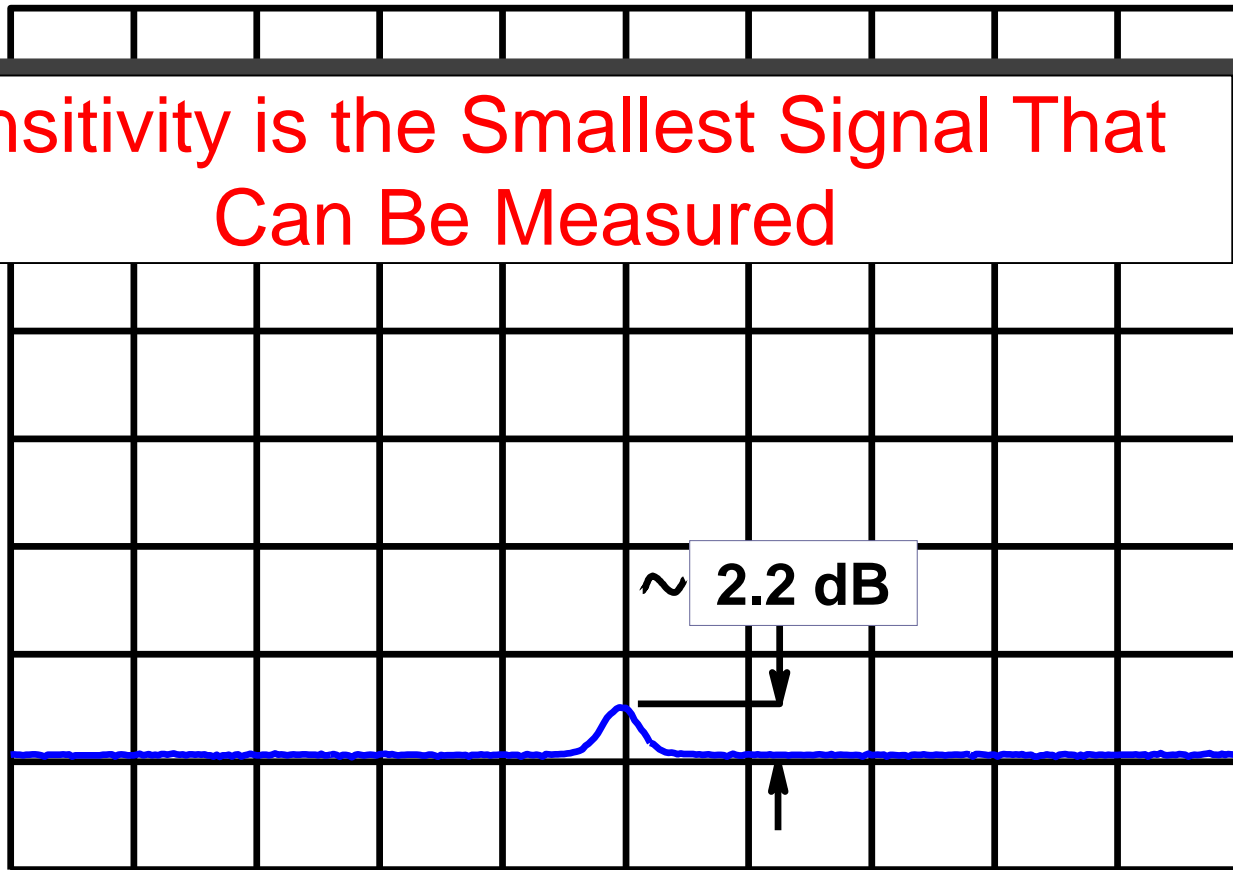


# Specifications

## Sensitivity/DANL

Sensitivity is the Smallest Signal That Can Be Measured

Signal  
Equals  
Noise



# Specifications

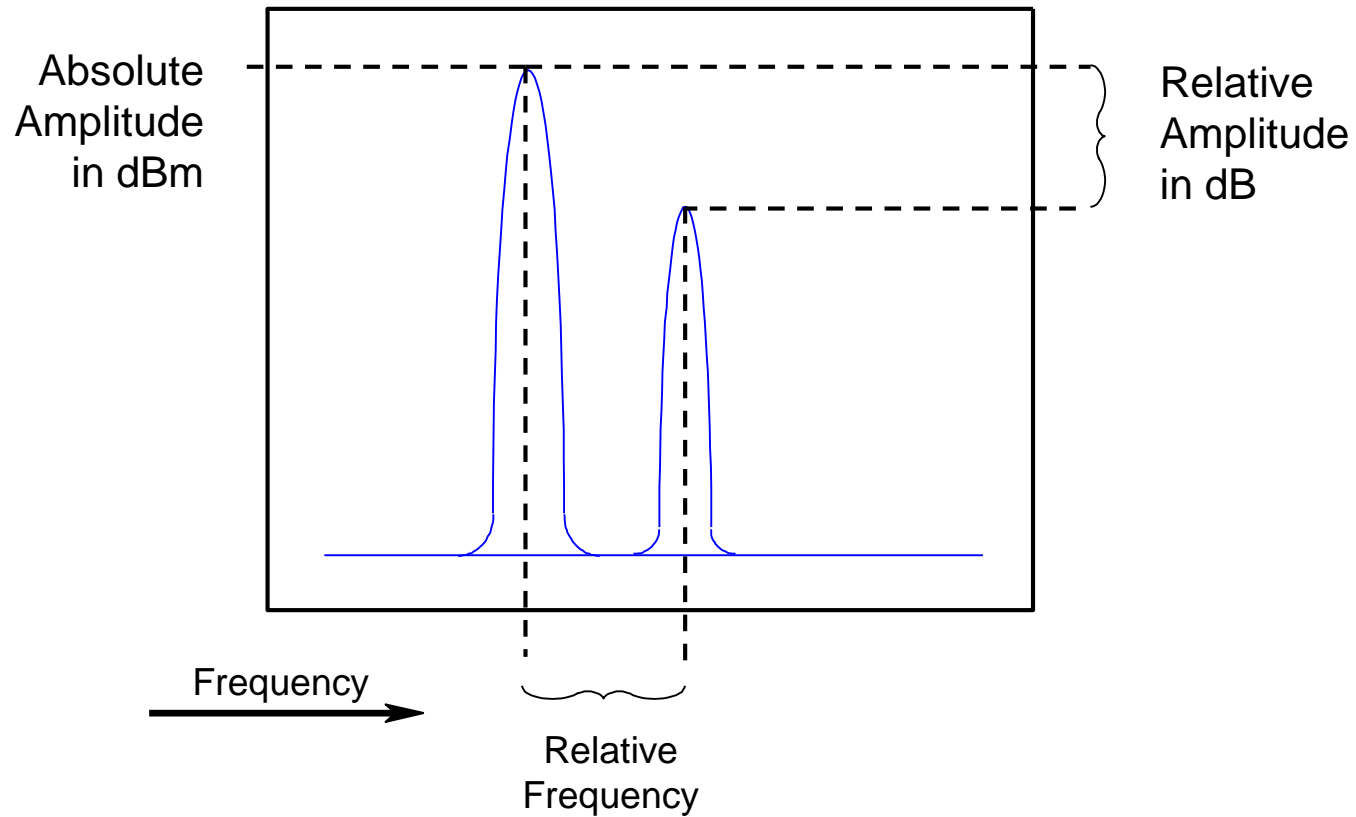
## Sensitivity/DANL

**For Best Sensitivity Use:**

- 👉 **Narrowest Resolution BW**
- 👉 **Minimum RF Input Attenuation**
- 👉 **Sufficient Video Filtering  
(Video BW < .01 Res BW)**

# Specifications

## Accuracy





# Specifications

Accuracy: Frequency Readout Accuracy

Typical datasheet specification:

Spans < 2 MHz:  $\pm$  (freq. readout x freq. ref. accuracy  
+ 1% of frequency span  
+ 15% of resolution bandwidth  
+ 10 Hz "residual error")



# Specifications

## Accuracy: Frequency Readout Accuracy Example

### Single Marker Example:

2 GHz

400 kHz span

3 kHz RBW

Calculation:	$(2 \times 10^9 \text{ Hz}) \times (1.3 \times 10^{-7} \text{ /yr.ref.error})$	=	260 Hz
	1% of 400 kHz span	=	4000 Hz
	15% of 3 kHz RBW	=	450 Hz
	10 Hz residual error	=	10 Hz
		Total =	$\pm 4720 \text{ Hz}$

# Specifications

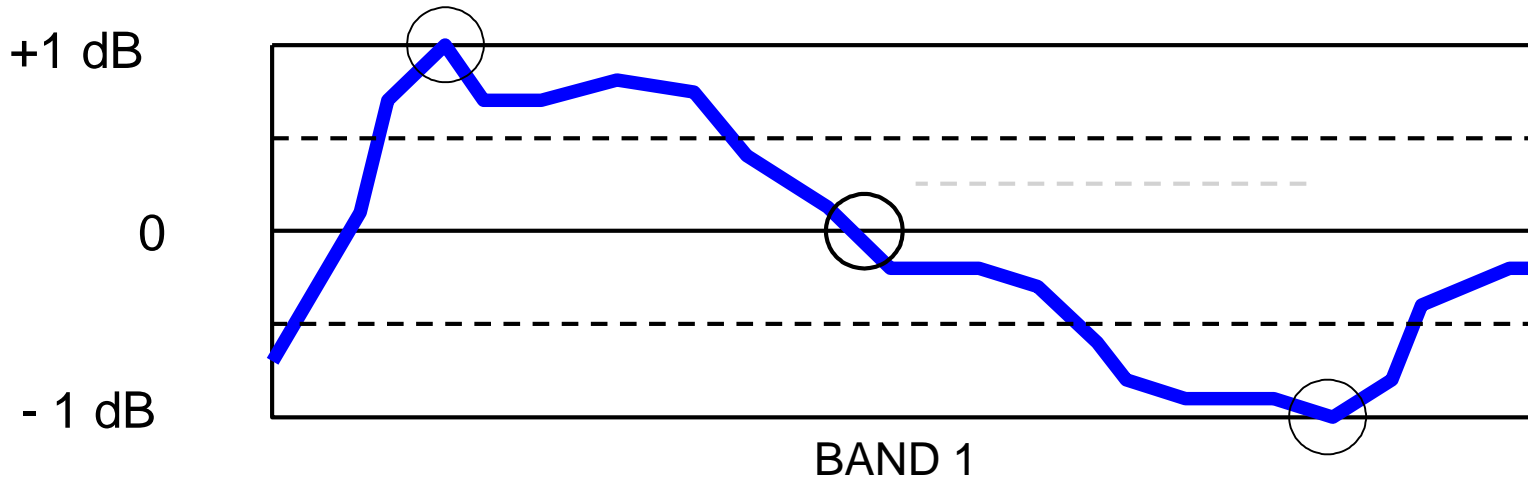
Accuracy: Relative Amplitude Accuracy

- **Display fidelity**
- **Frequency response**
  - **RF Input attenuator**
  - **Reference level**
  - **Resolution bandwidth**
  - **Display scaling**

# Specifications

Accuracy: Relative Amplitude Accuracy - Freq. Response

## Signals in the Same Harmonic Band



**Specification:  $\pm 1$  dB**

# Specifications

Accuracy: Relative Amplitude Accuracy

- **RF Input attenuator**
- **Reference level**
- **Resolution bandwidth**
- **Display scaling**

# Specifications

Accuracy: Absolute Amplitude Accuracy

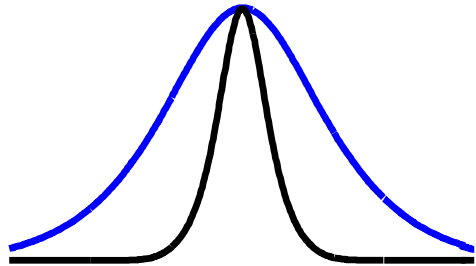
Absolute  
Amplitude  
in dBm

- **Calibrator accuracy**
- **Frequency response**
- **Reference level uncertainty**

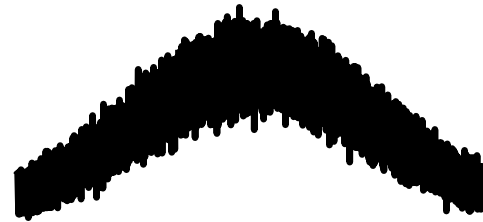
# Specifications

## Resolution

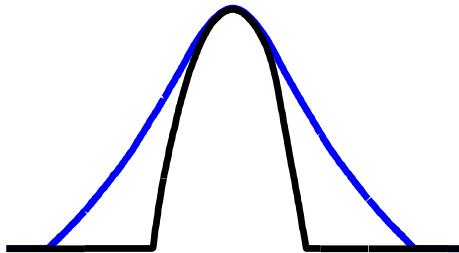
### What Determines Resolution?



Resolution  
Bandwidth



Residual FM



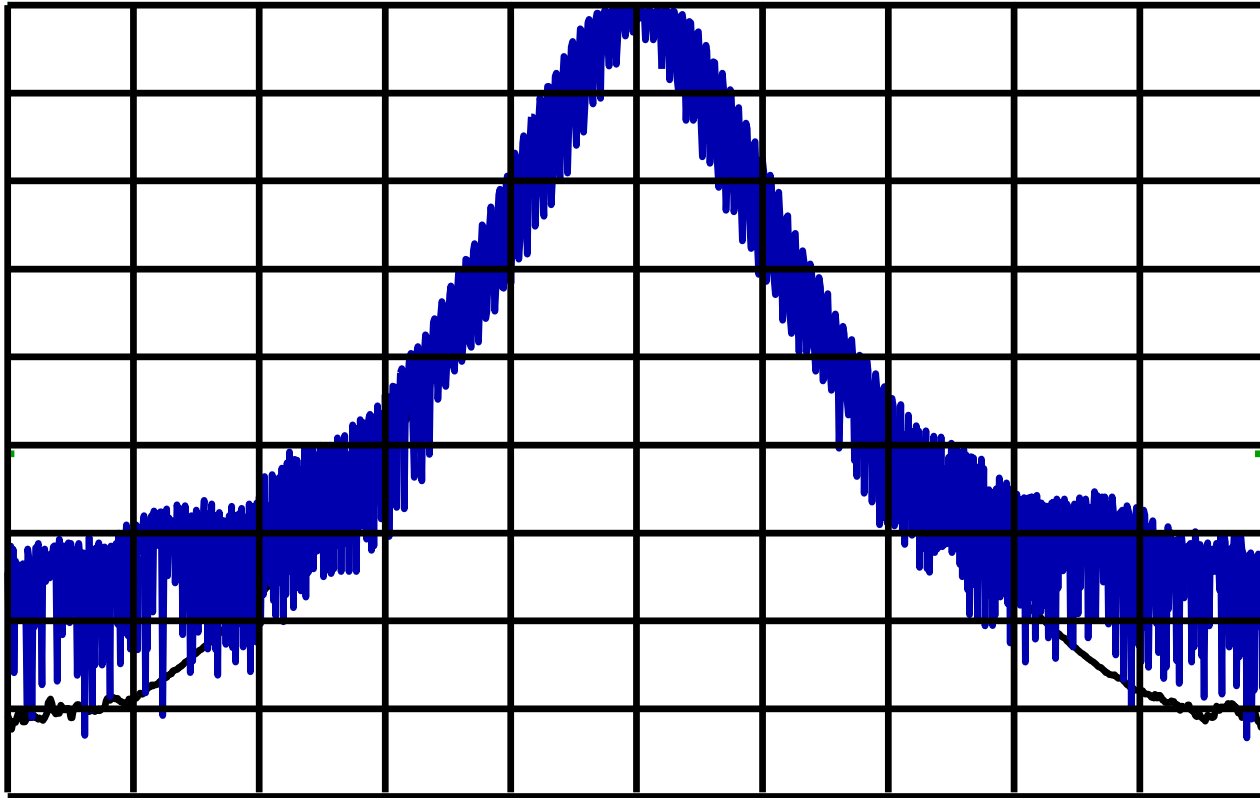
RBW Type and  
Selectivity



Noise Sidebands

# Specifications

Resolution: Residual FM

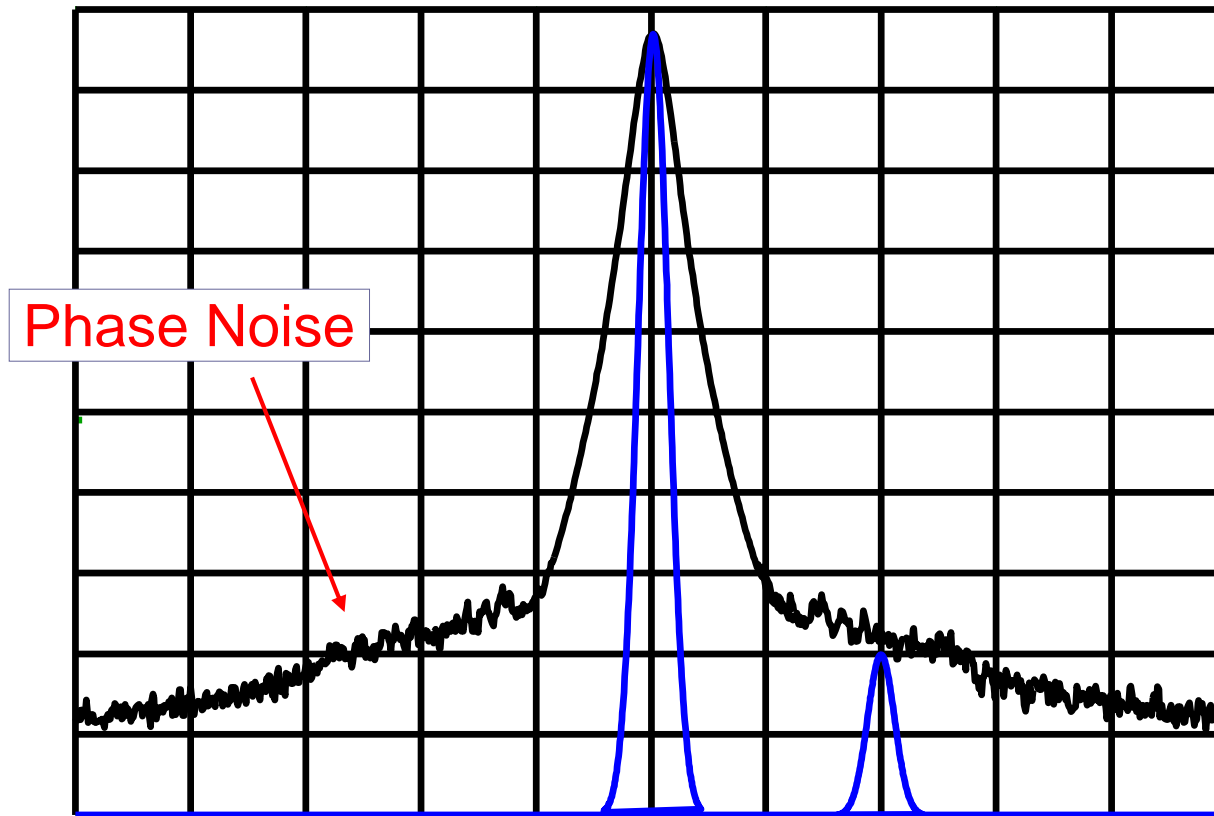


Residual FM  
"Smears" the Signal



# Specifications

Resolution: Noise Sidebands

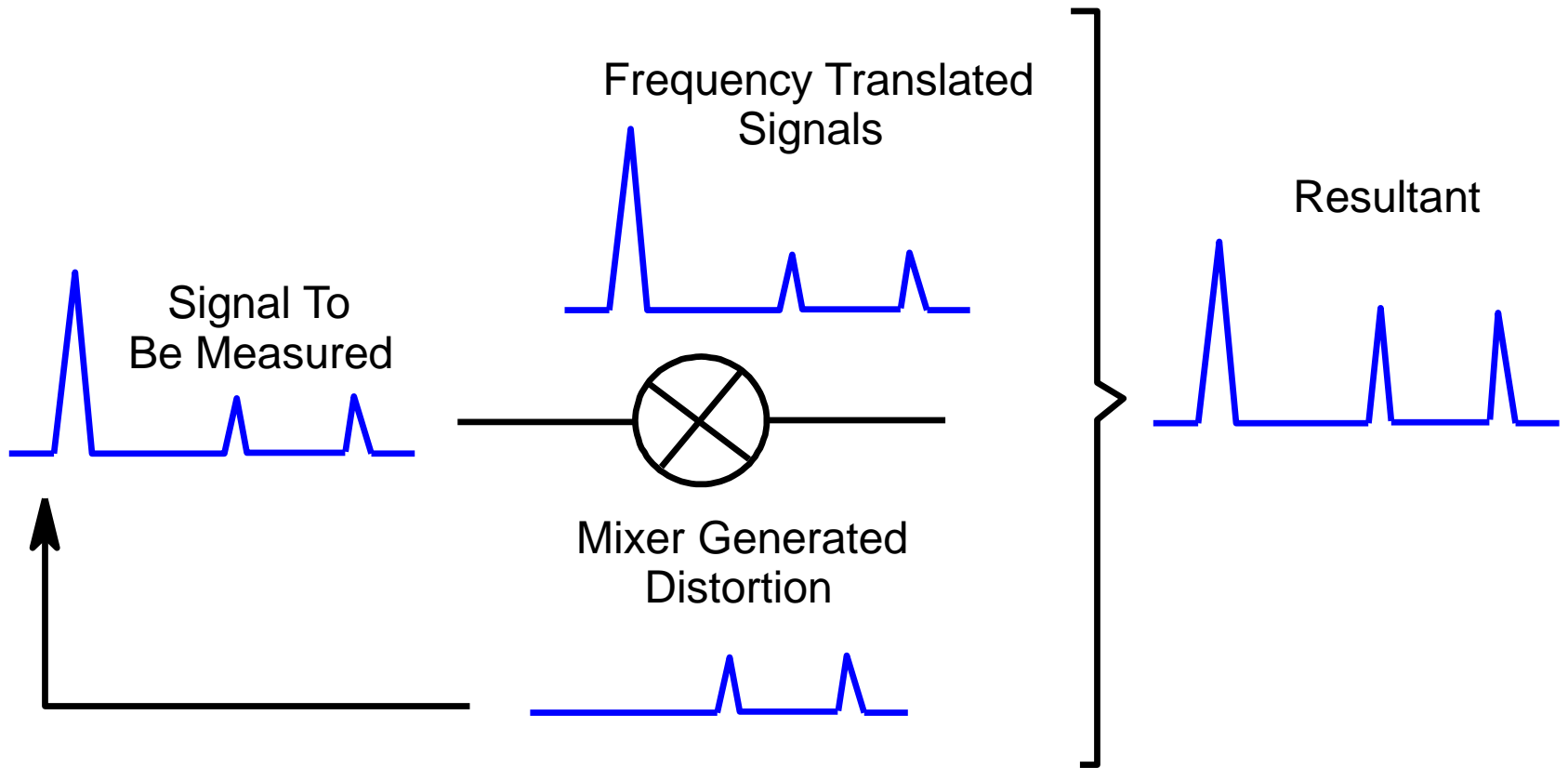


Noise Sidebands can prevent resolution of unequal signals

# Specifications

## Distortion

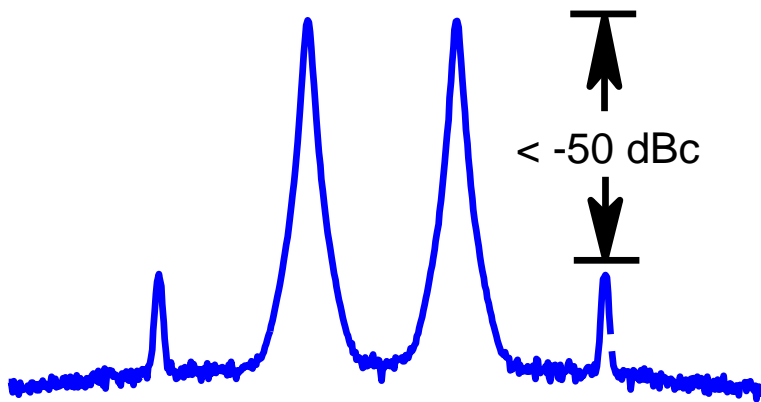
### Mixers Generate Distortion



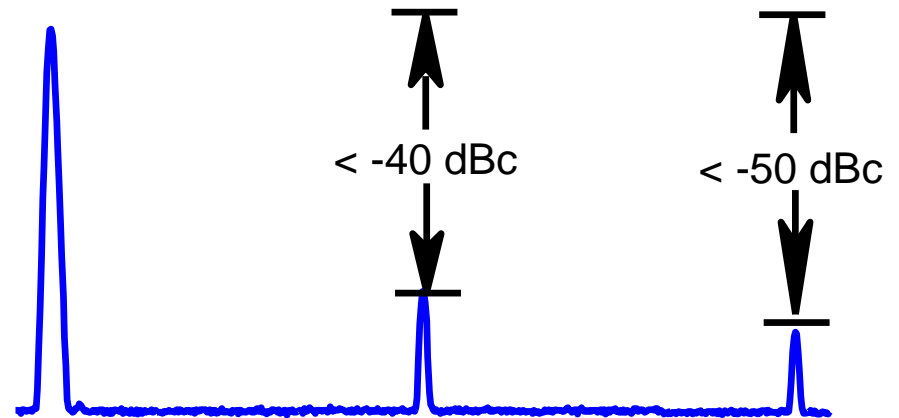
# Specifications

## Distortion

Most Influential Distortion is the Second and Third Order



Two-Tone Intermod

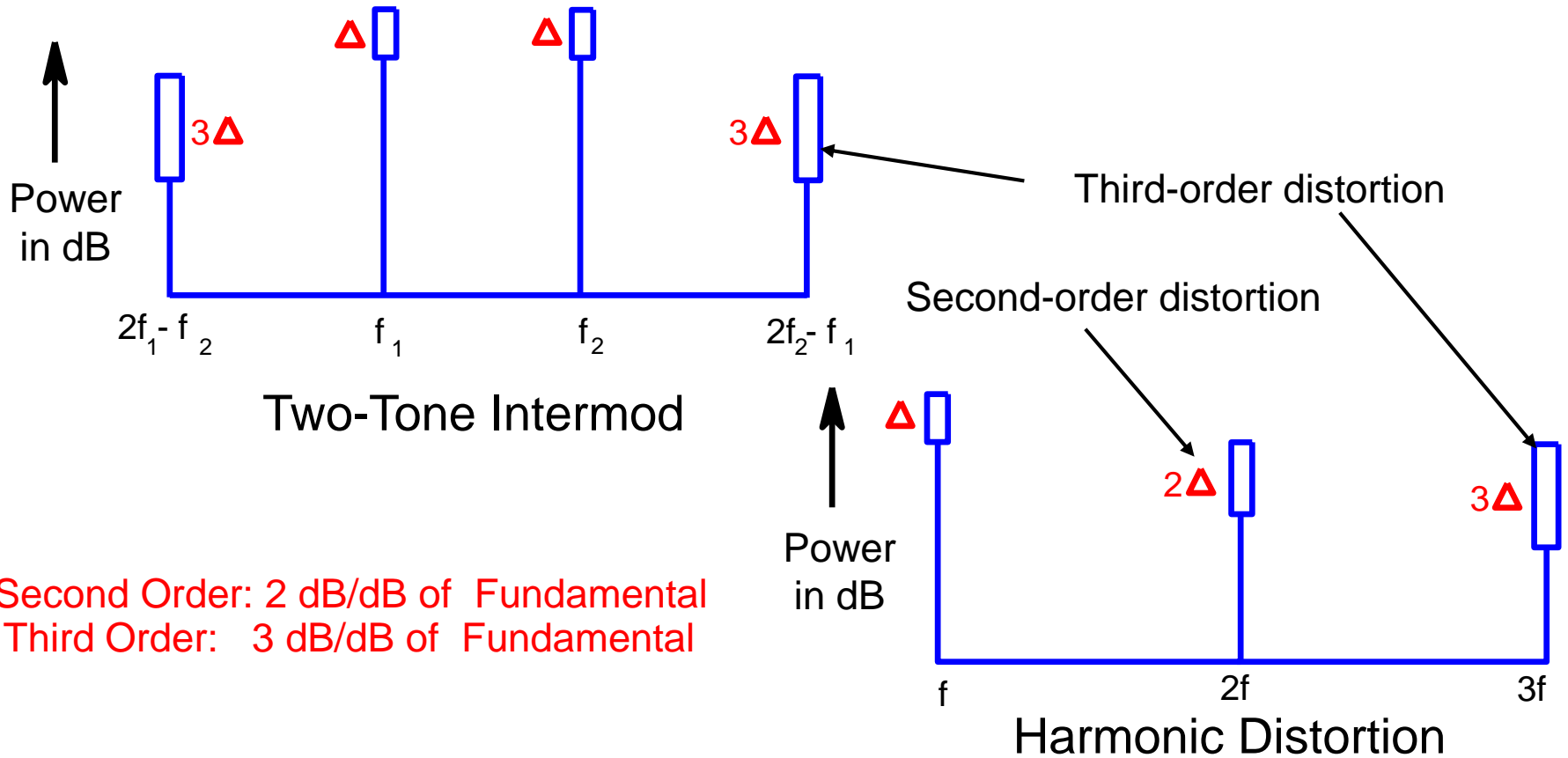


Harmonic Distortion

# Specifications

## Distortion

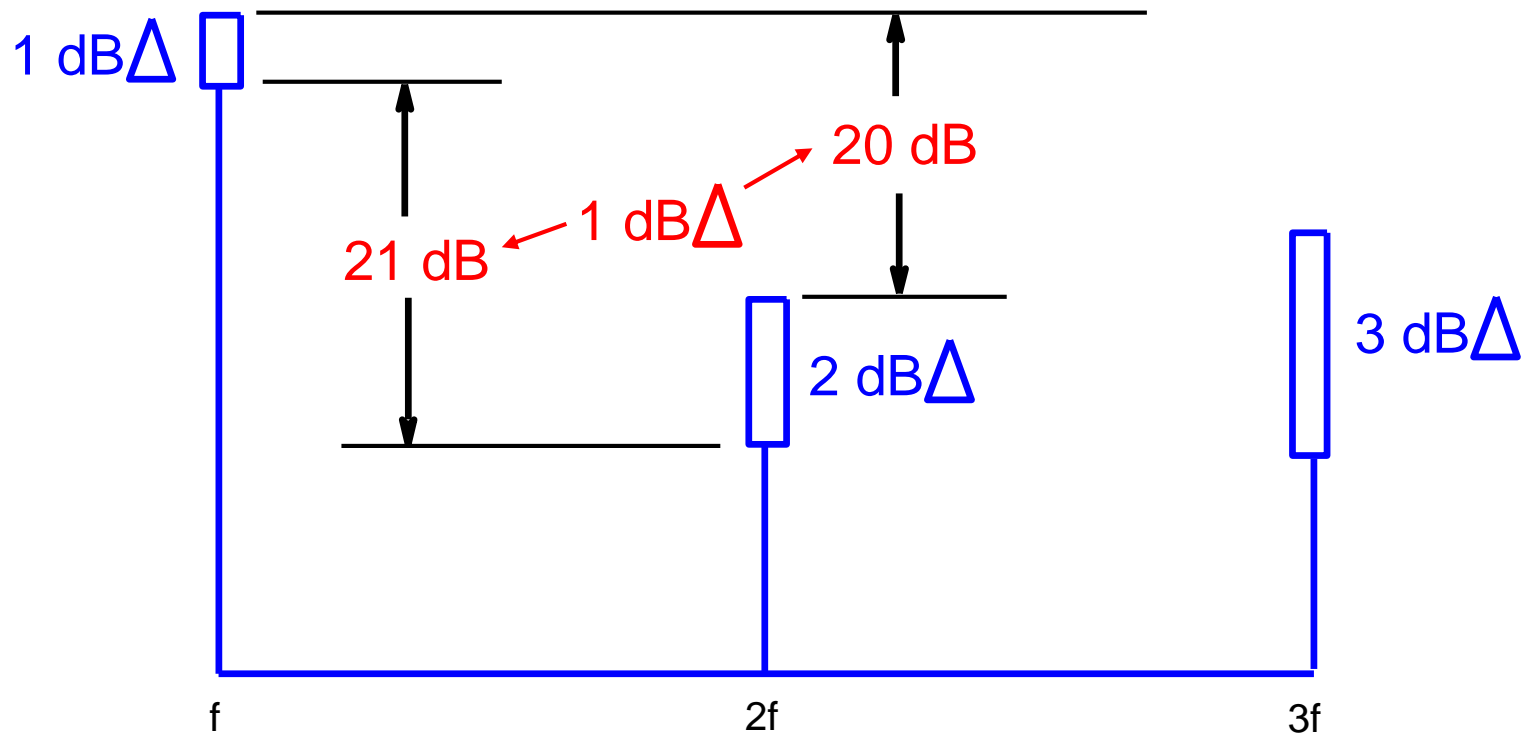
### Distortion Products Increase as a Function of Fundamental's Power



# Specifications

## Distortion

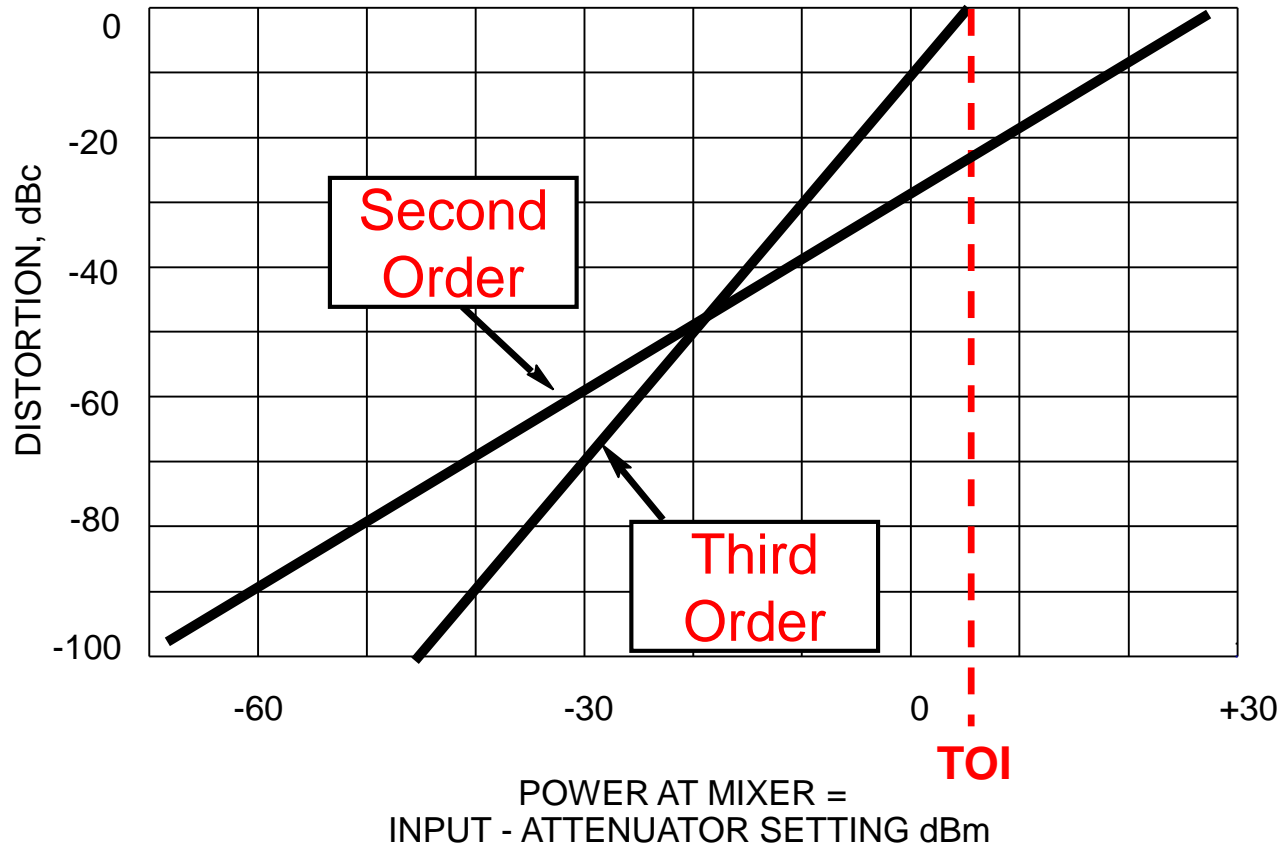
### Relative Amplitude Distortion Changes with Input Power Level



# Specifications

## Distortion

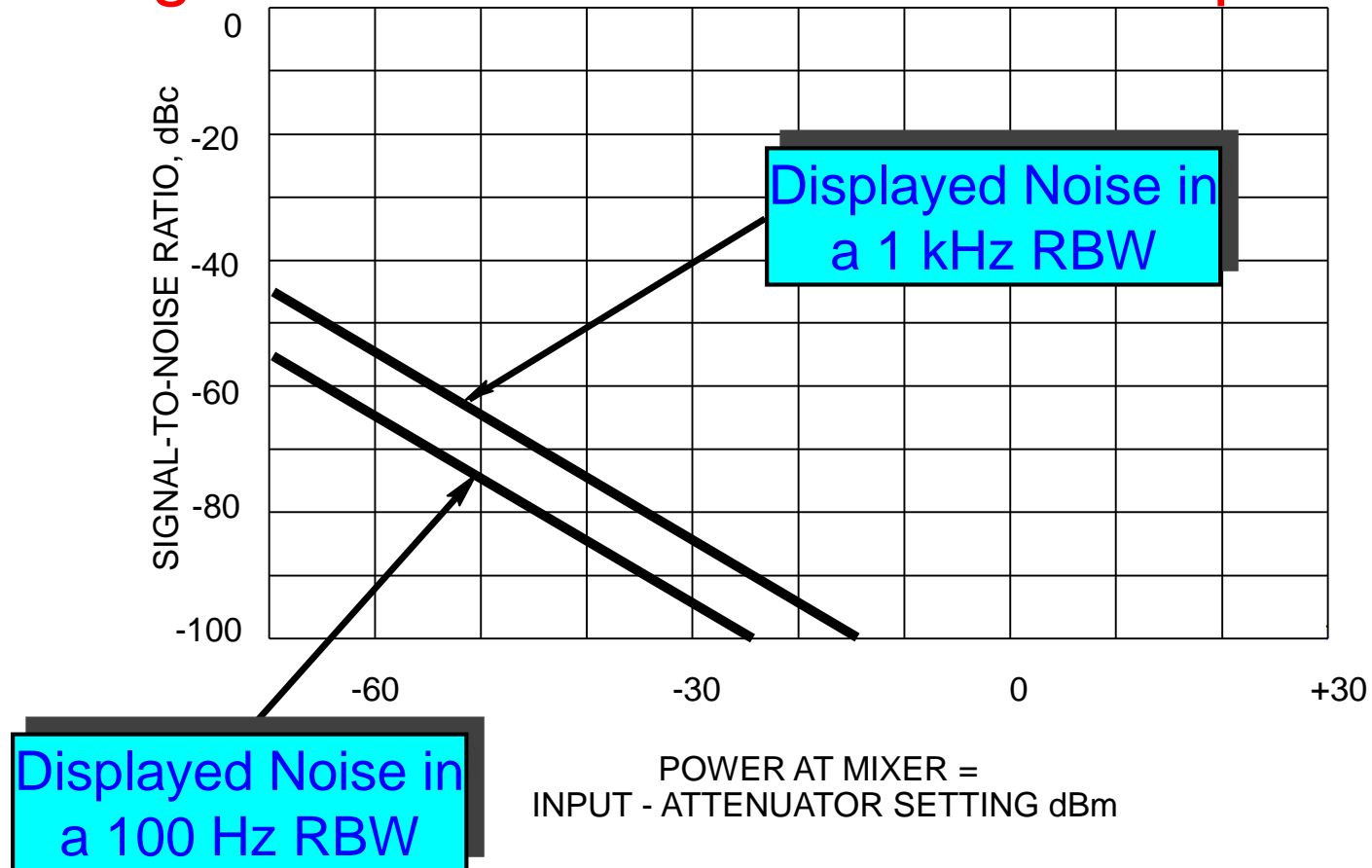
Distortion is a Function of Mixer Level



# Specifications

## Dynamic Range

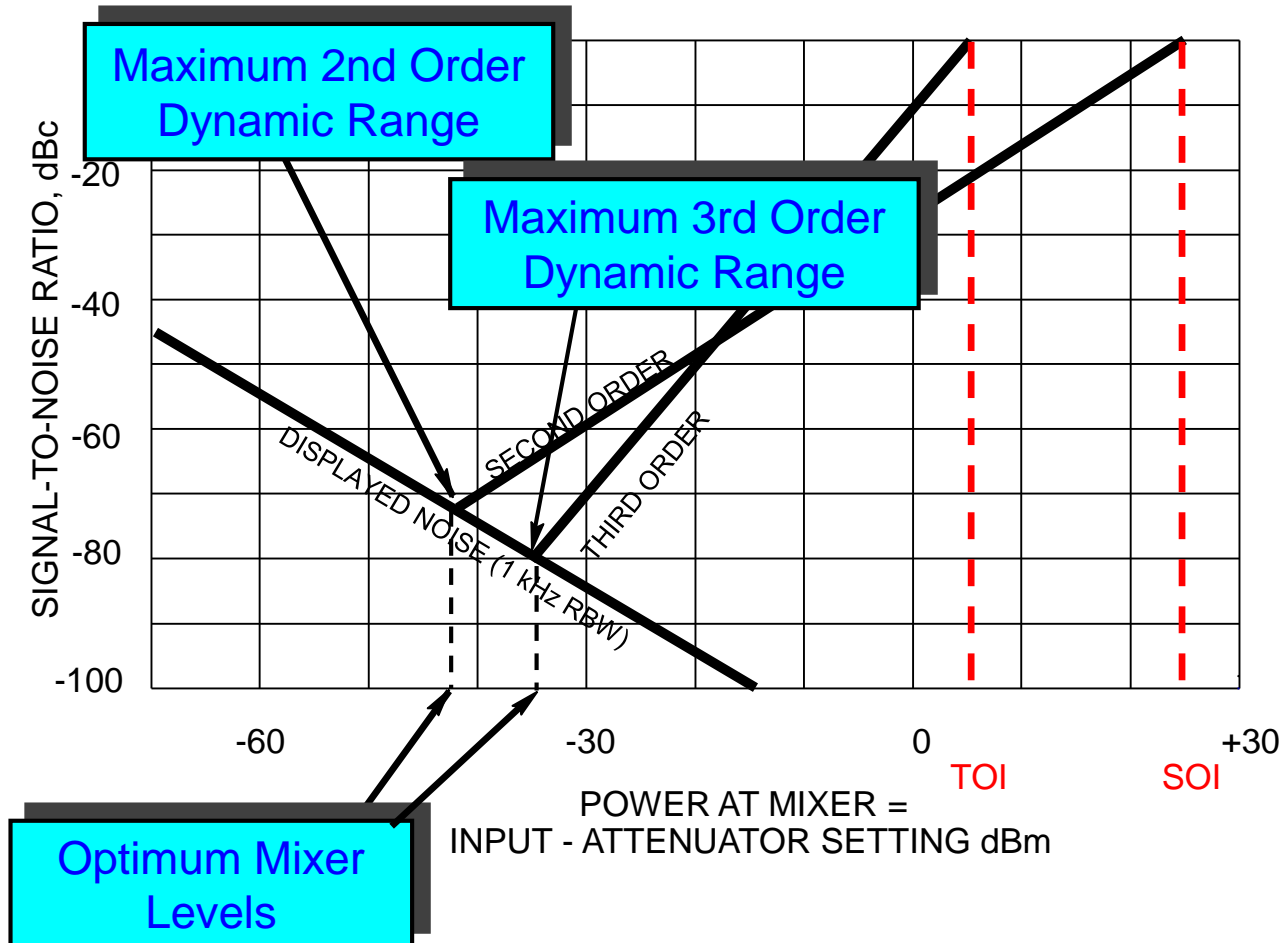
### Signal-to-Noise Ratio Can Be Graphed



# Specifications

## Dynamic Range

Dynamic Range Can Be Presented Graphically

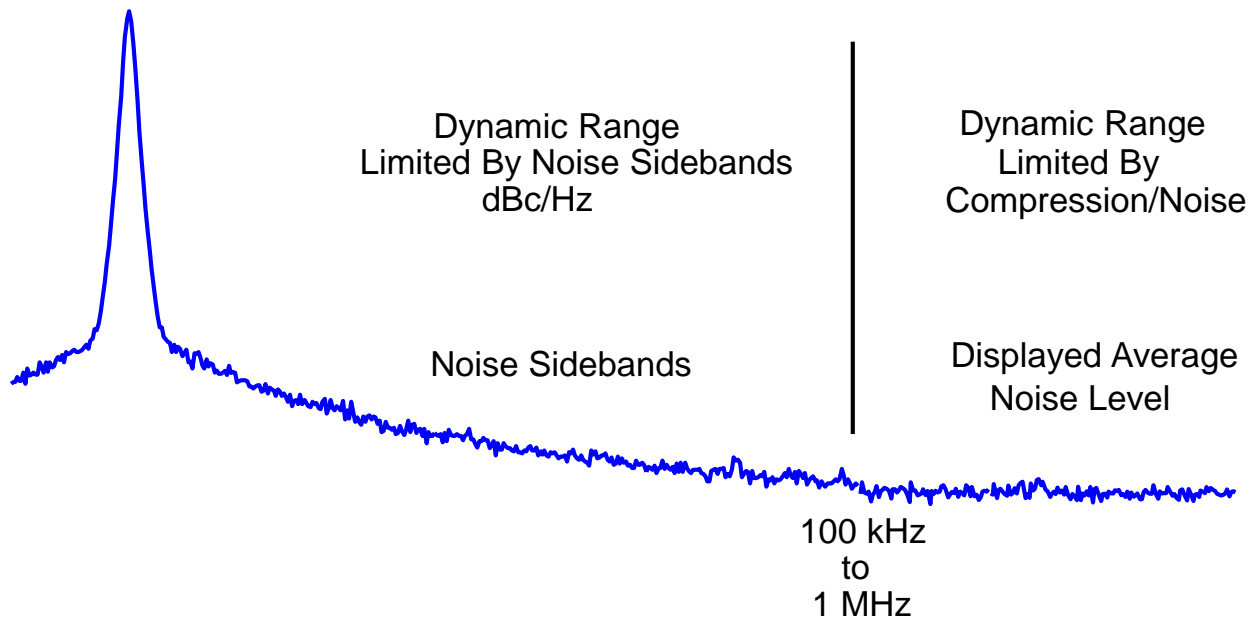




# Specifications

## Dynamic Range

### Dynamic Range for Spur Search Depends on Closeness to Carrier



# Specifications

## Dynamic Range

Actual Dynamic Range is the Minimum of:

Maximum dynamic range calculation

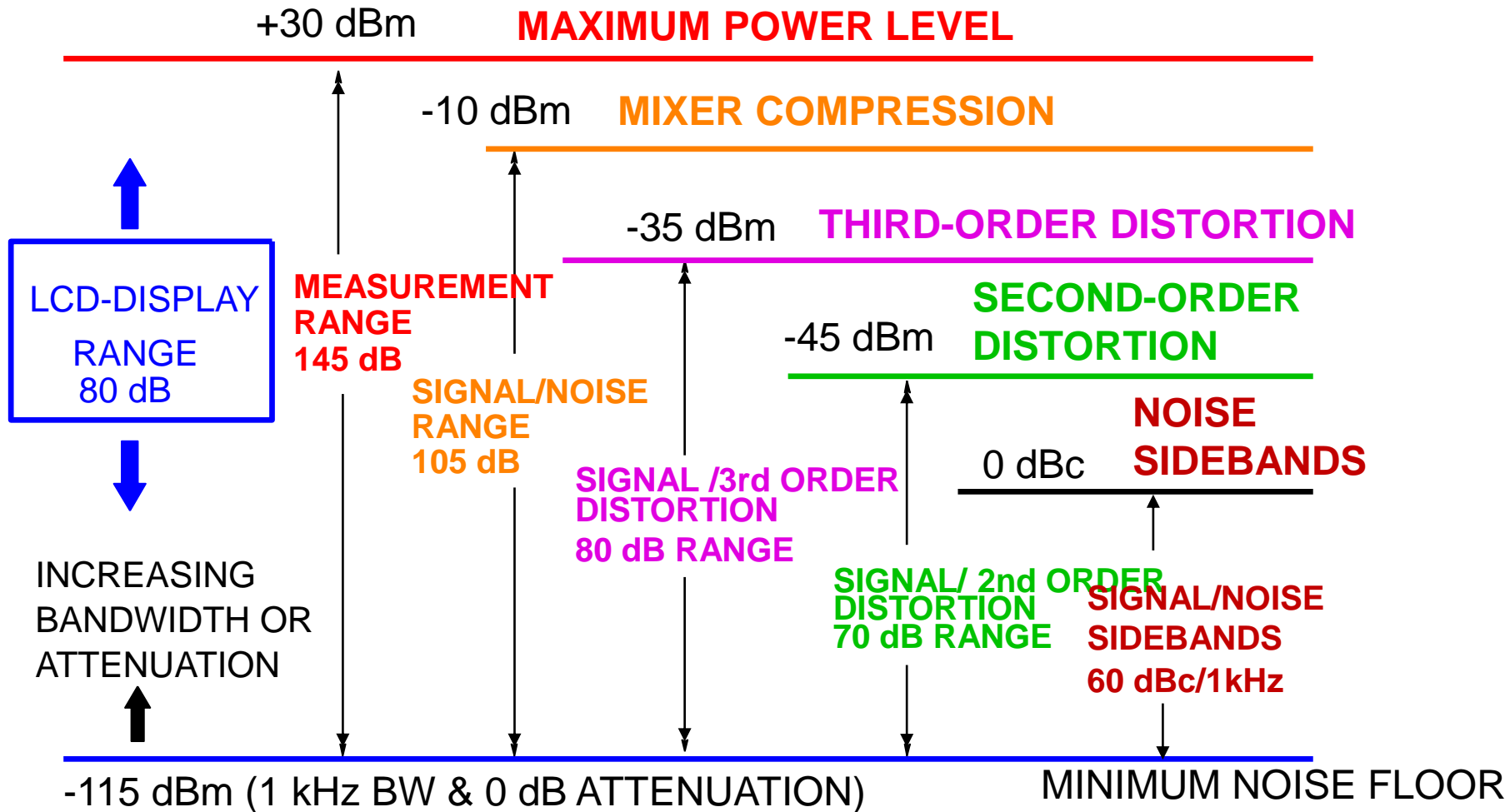
Calculated from:

- ▲ distortion
- ▲ sensitivity

Noise sidebands at the offset frequency

# Specifications

## Dynamic Range

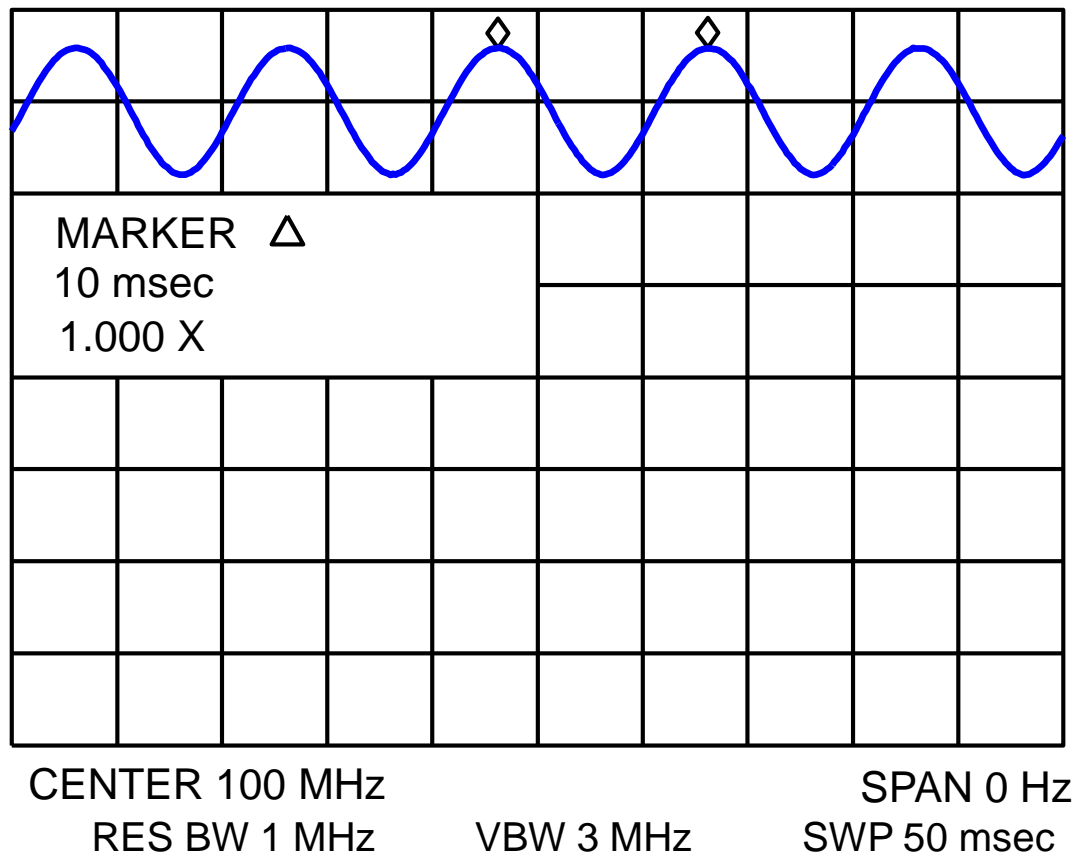


# SPAN ZERO

## Modulation Measurements: Time Domain

It was mentioned briefly that although a spectrum analyzer is primarily used to view signals in the frequency domain, it is also possible to use the spectrum analyzer to look at the time domain. This is done with a feature called zero-span. This is useful for determining modulation type or for demodulation.

The spectrum analyzer is set for a frequency span of zero (hence the term zero-span) with some nonzero sweep time. The center frequency is set to the carrier frequency and the resolution bandwidth must be set large enough to allow the modulation sidebands to be included in the measurement. The analyzer will plot the amplitude of the signal versus time, within the limitations of its detector and video and RBWs.



# Specifications

## Frequency Range

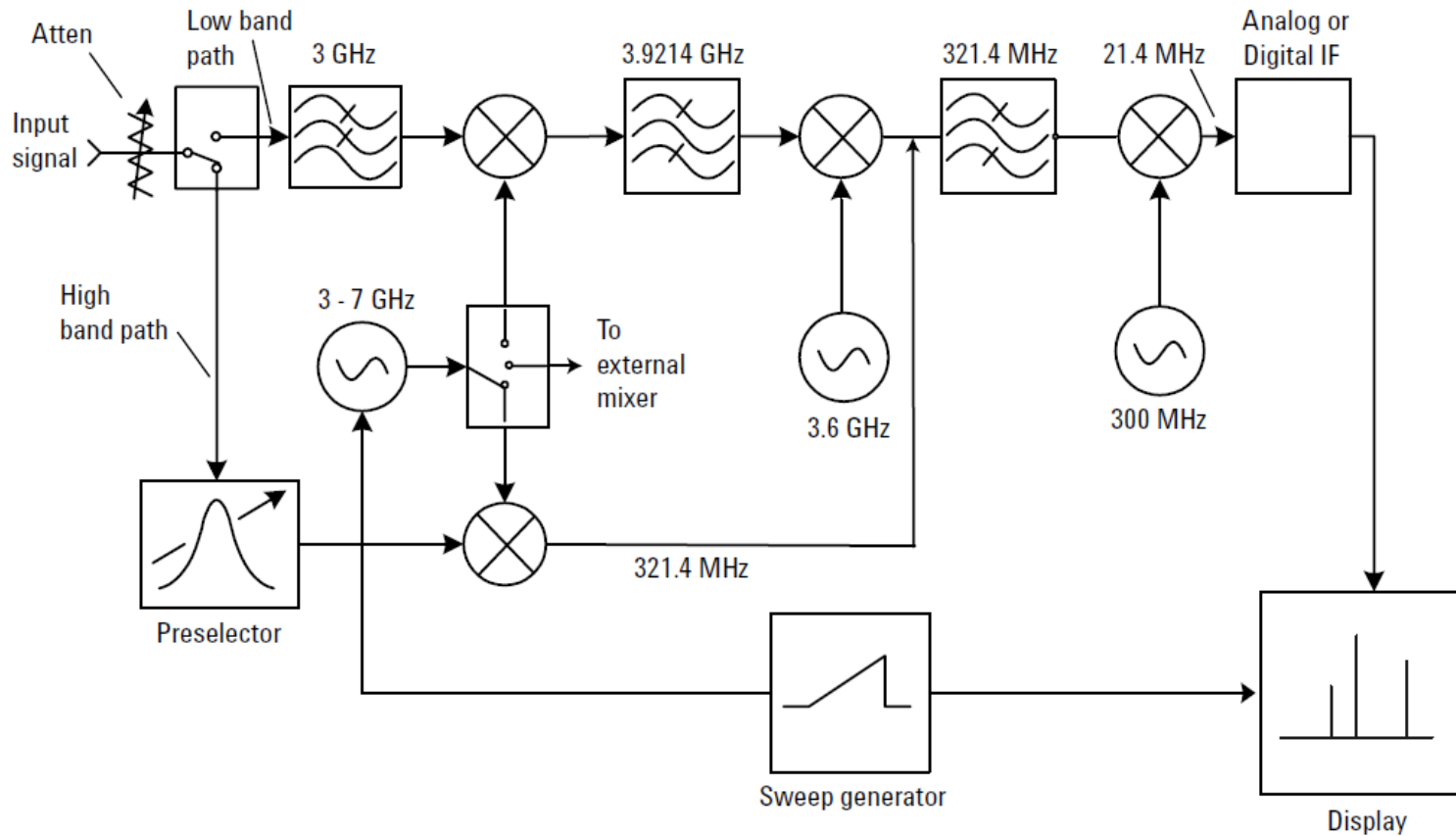


Low frequencies  
for baseband and IF

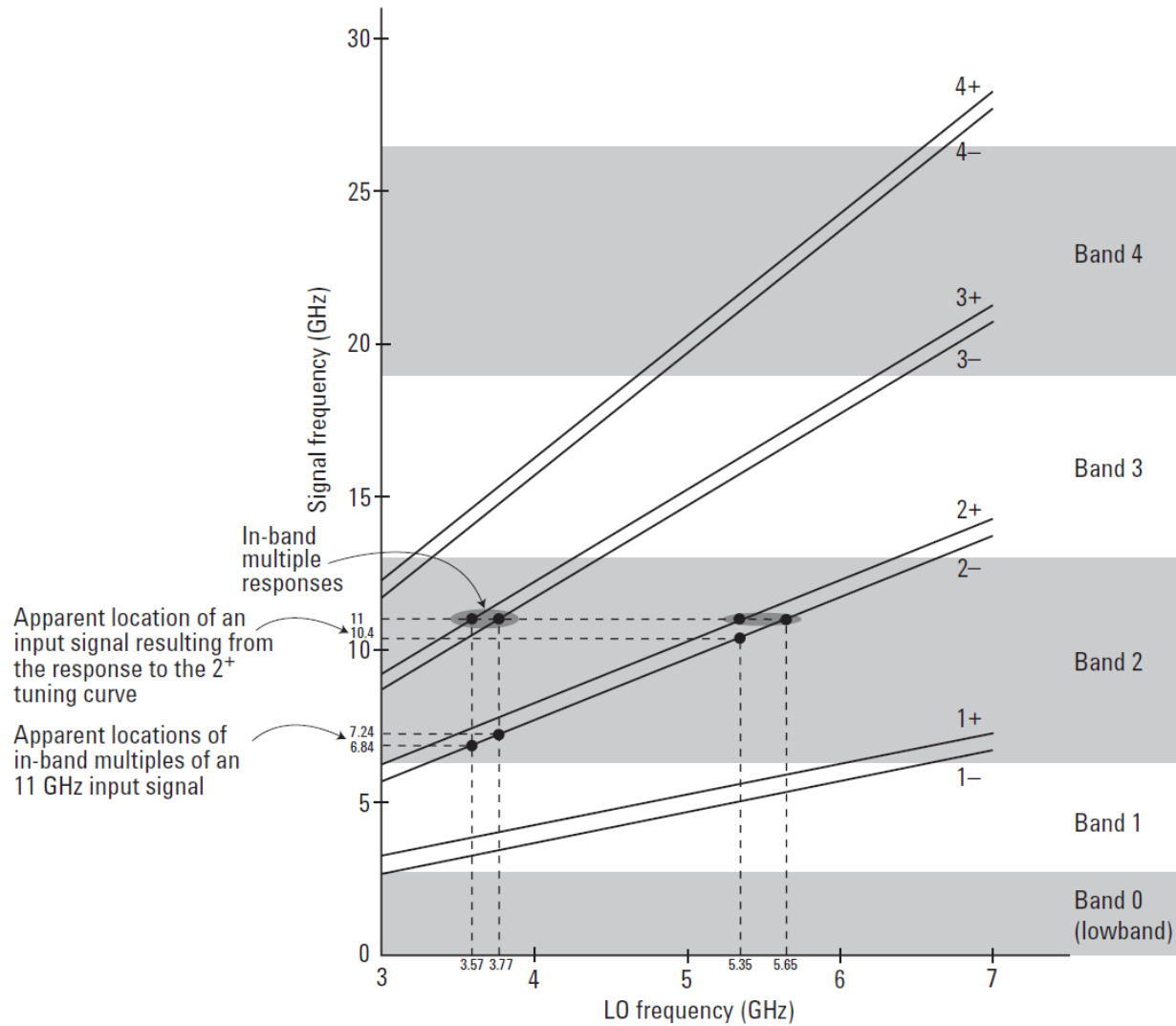


Measuring harmonics  
50 GHz and beyond!

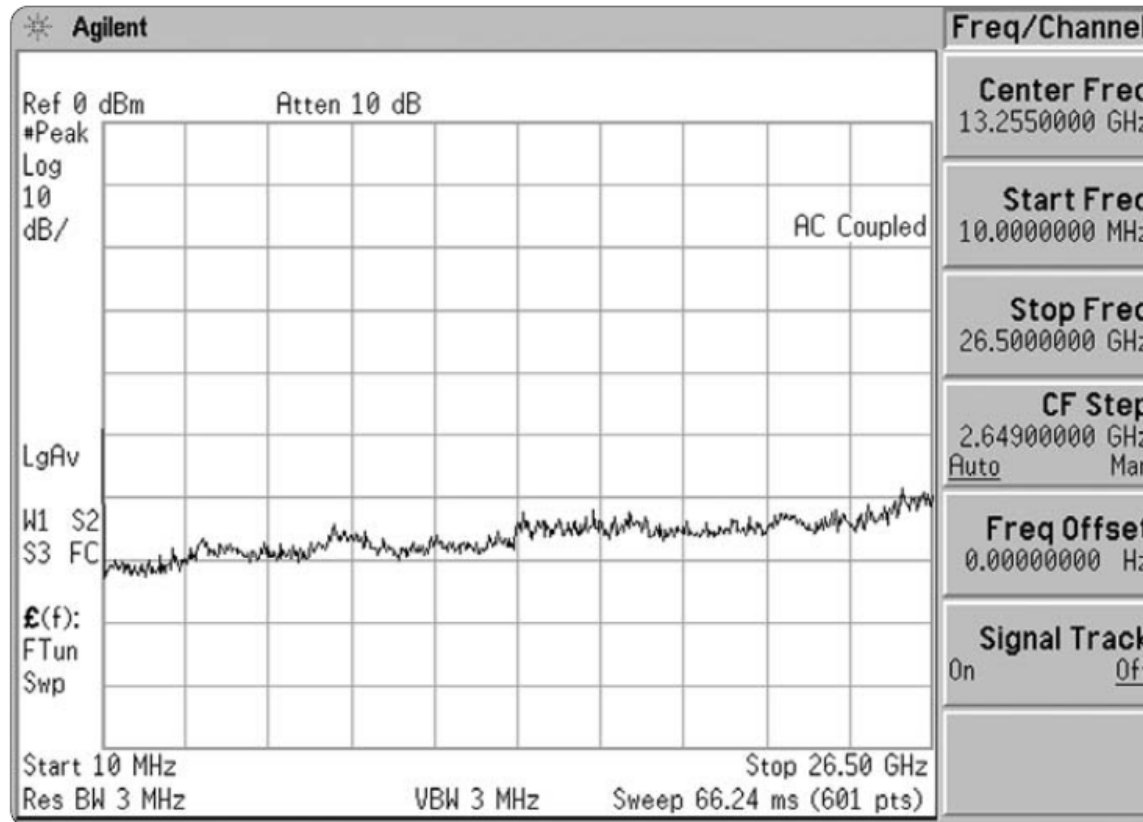
# Higher Bands



# LO Harmonics



# Noise level for higher bands



**Figure 7-9. Rise in noise floor indicates changes in sensitivity with changes in LO harmonic used**





# External Mixer

**Table 7-1. Harmonic mixing modes used by ESA-E and PSA Series with external mixers**

Band	Harmonic mixing mode (N <sup>a</sup> )	
	Preselected	Unpreselected
K (18.0 to 26.5 GHz)	n/a	6 <sup>-</sup>
A (26.5 to 40.0 GHz)	8 <sup>+</sup>	8 <sup>-</sup>
Q (33.0 to 50.0 GHz)	10 <sup>+</sup>	10 <sup>-</sup>
U (40.0 to 60.0 GHz)	10 <sup>+</sup>	10 <sup>-</sup>
V (50.0 to 75.0 GHz)	14 <sup>+</sup>	14 <sup>-</sup>
E (60.0 to 90.0 GHz)	n/a	16 <sup>-</sup>
W (75.0 to 110.0 GHz)	n/a	18 <sup>-</sup>
F (90.0 to 140.0 GHz)	n/a	20 <sup>-</sup>
D (110.0 to 170.0 GHz)	n/a	24 <sup>-</sup>
G (140.0 to 220.0 GHz)	n/a	32 <sup>-</sup>
Y (170.0 to 260.0 GHz)	n/a	38 <sup>-</sup>
J (220.0 to 325.0 GHz)	n/a	46 <sup>-</sup>

# Image shift

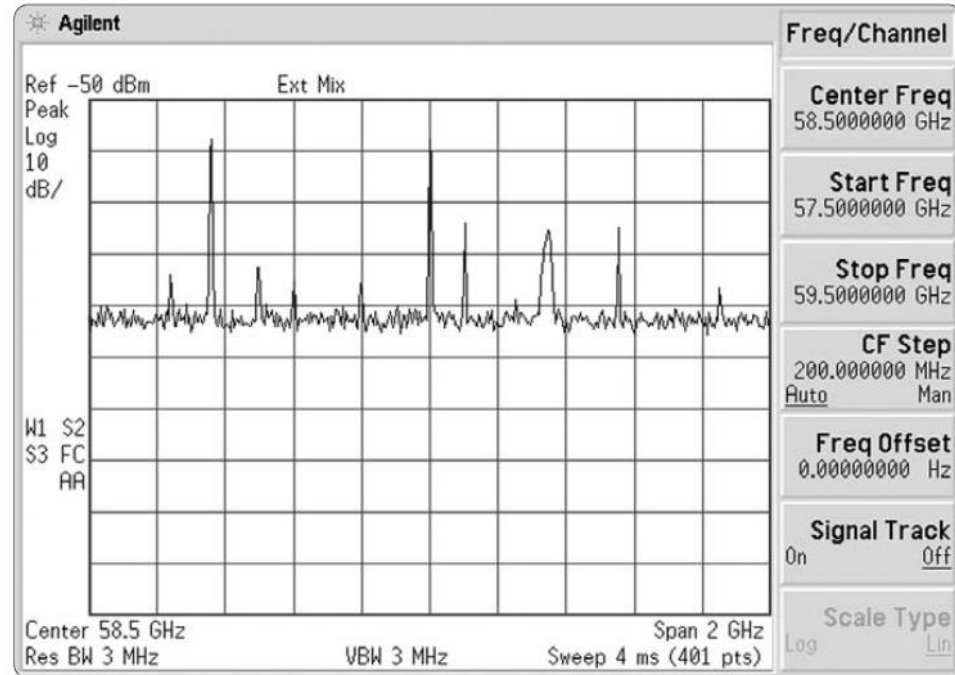
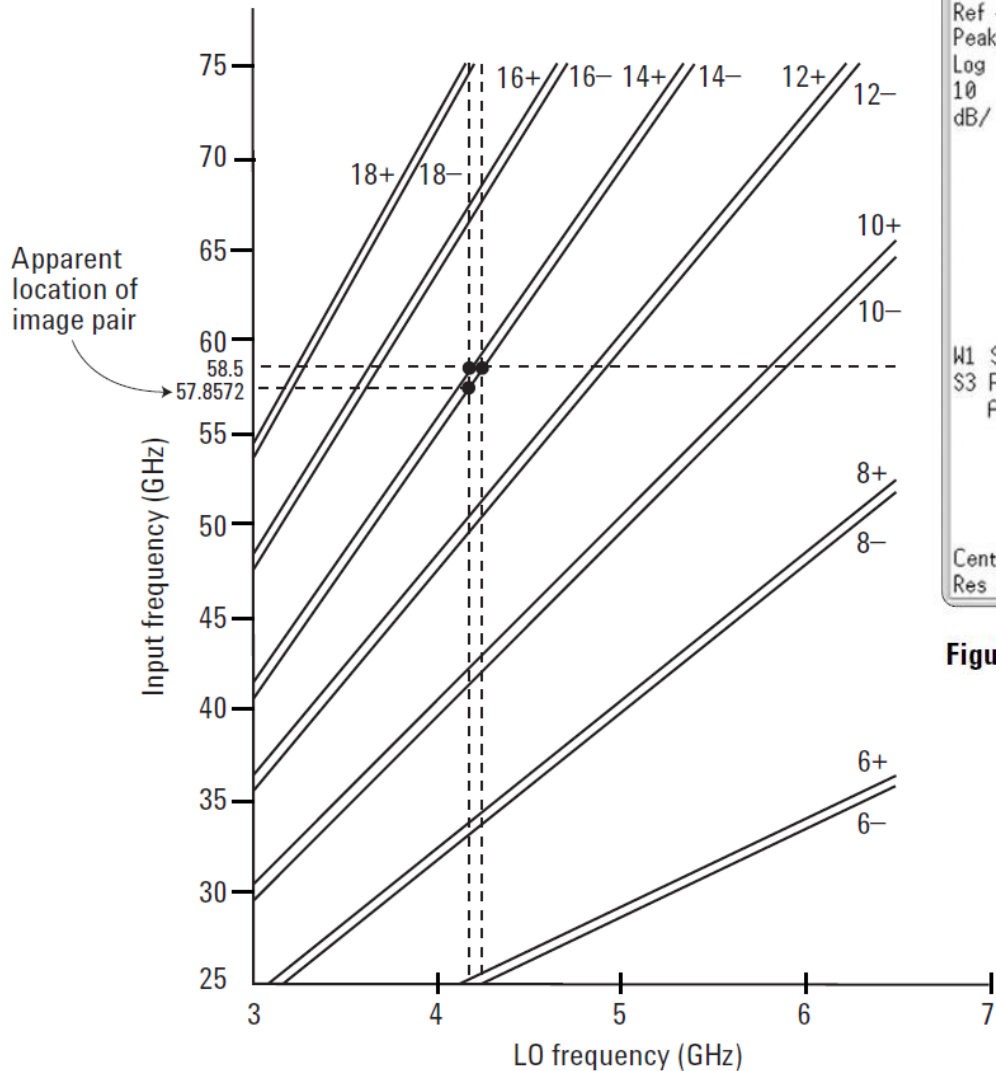
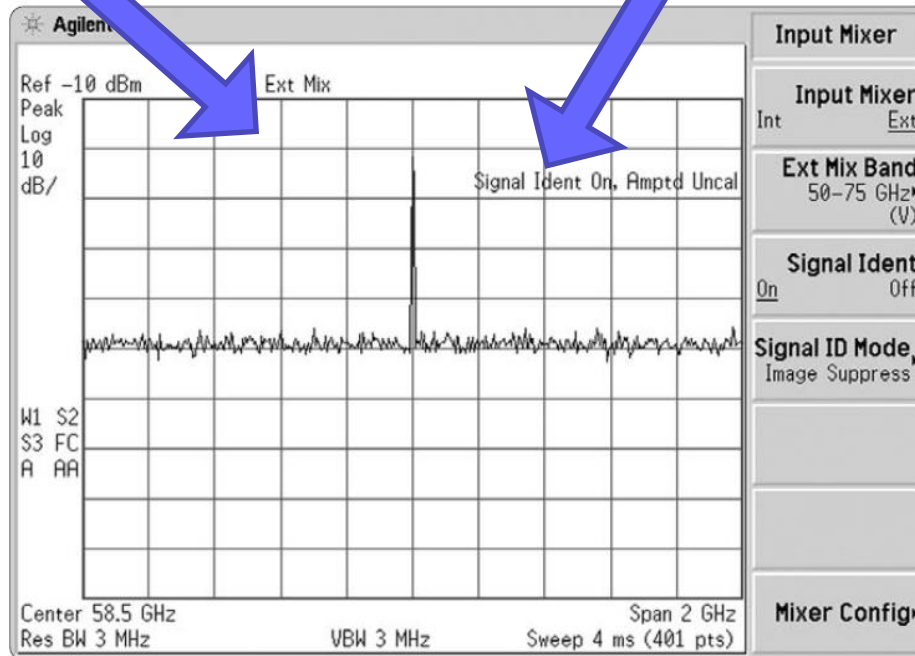
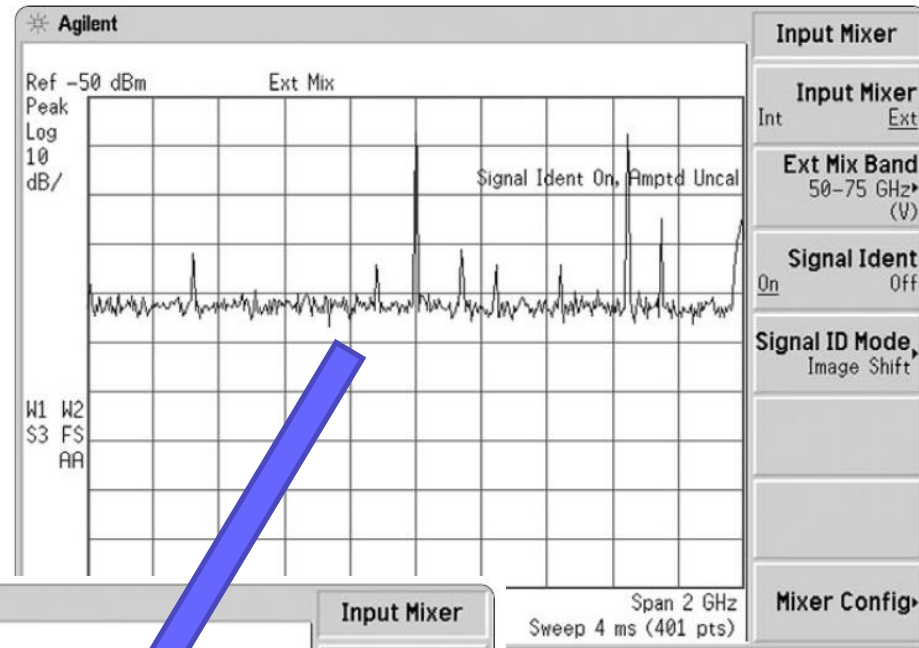
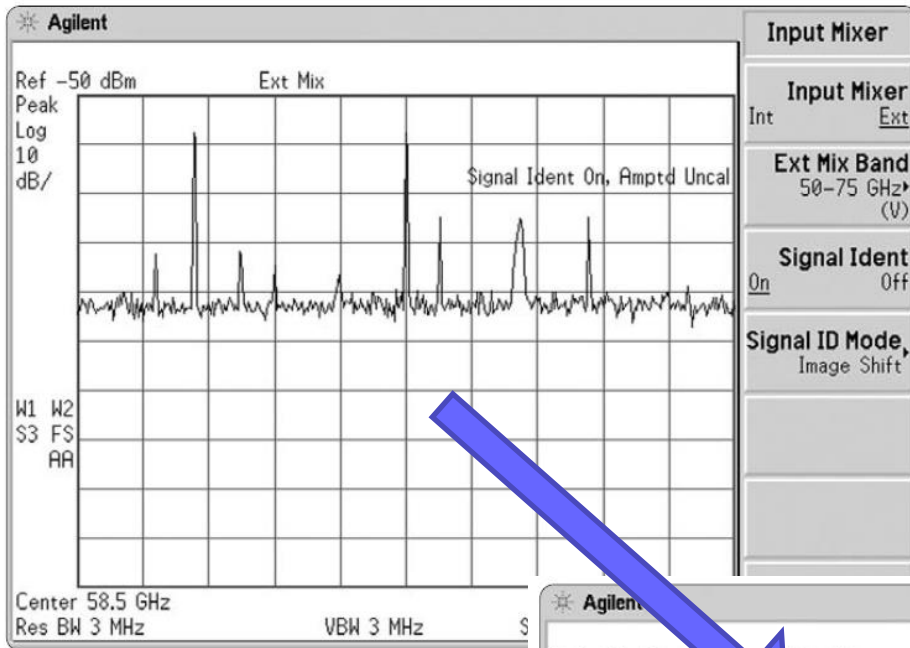


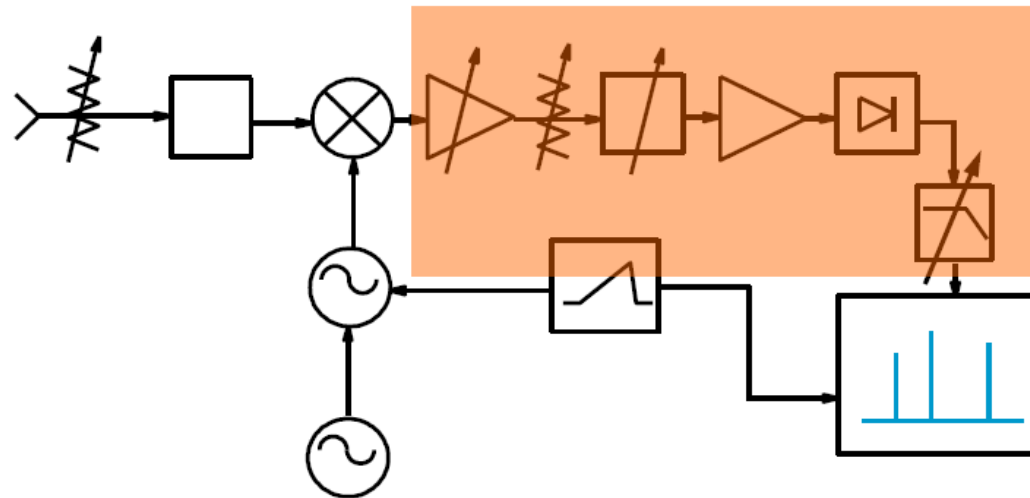
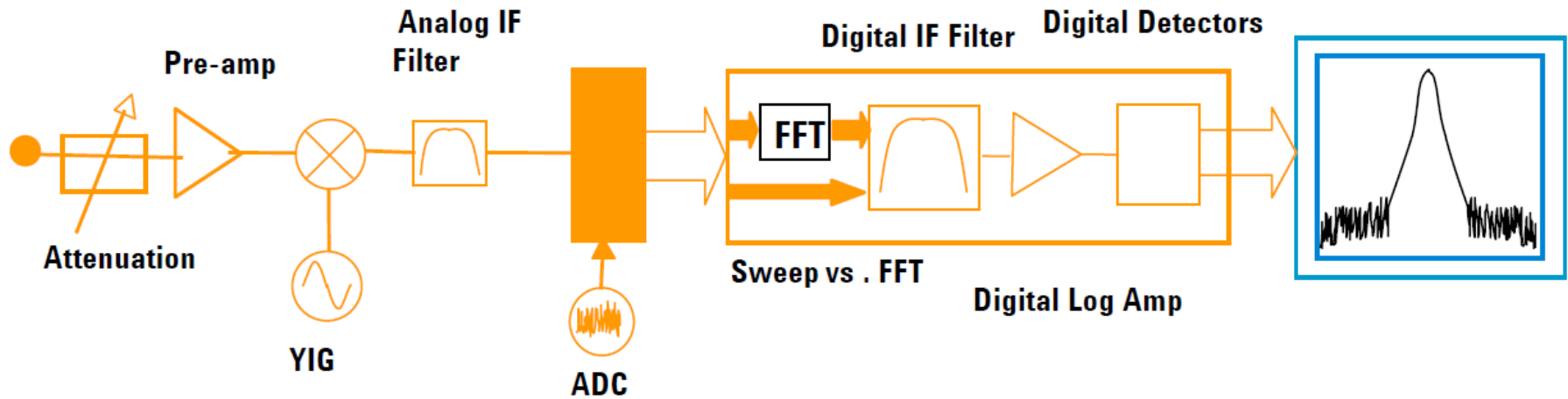
Figure 7-15. Which ones are the real signals?

# Image suppress

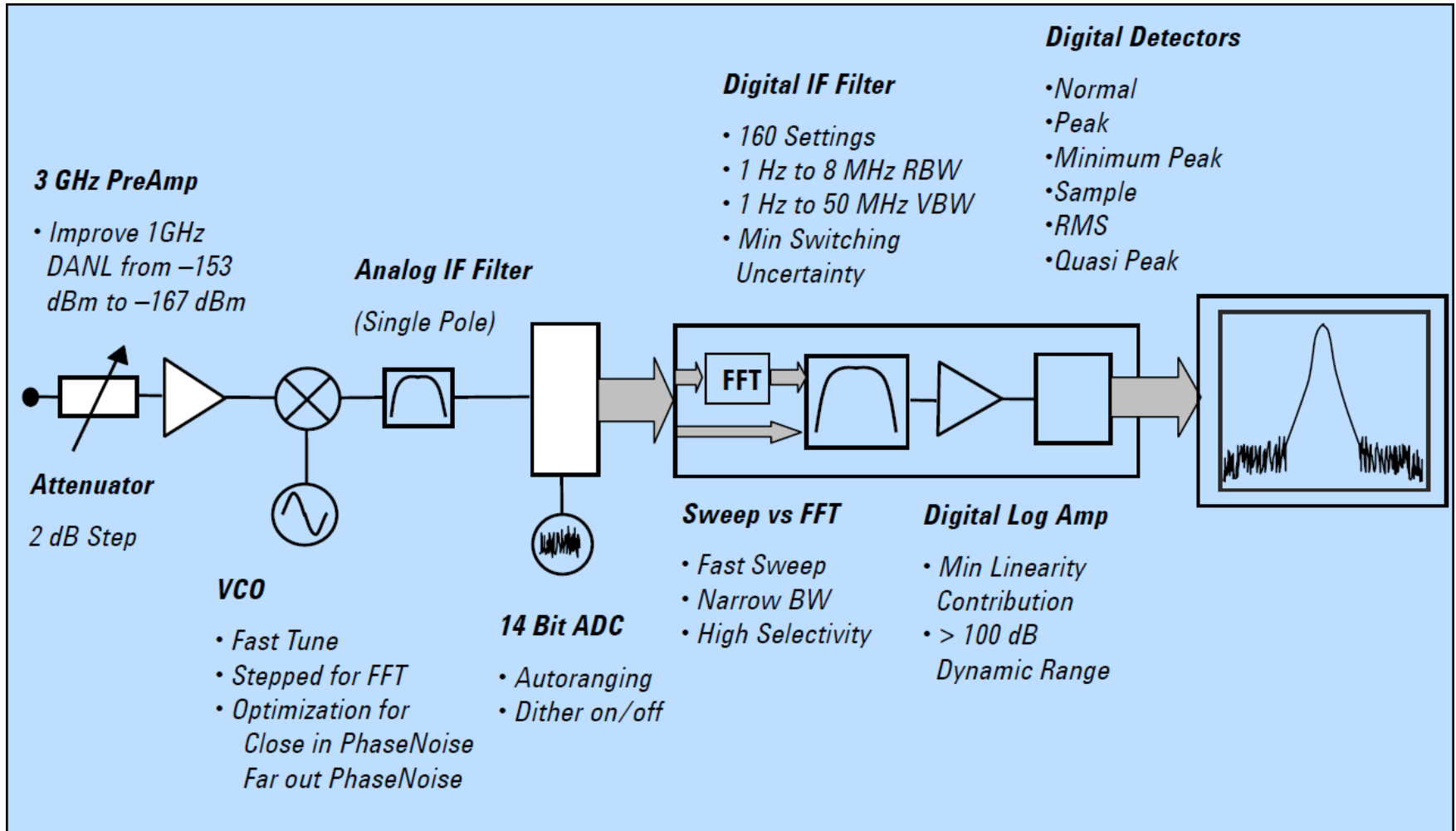


MIN HOLD  
function, which saves  
the smaller value of  
each display point

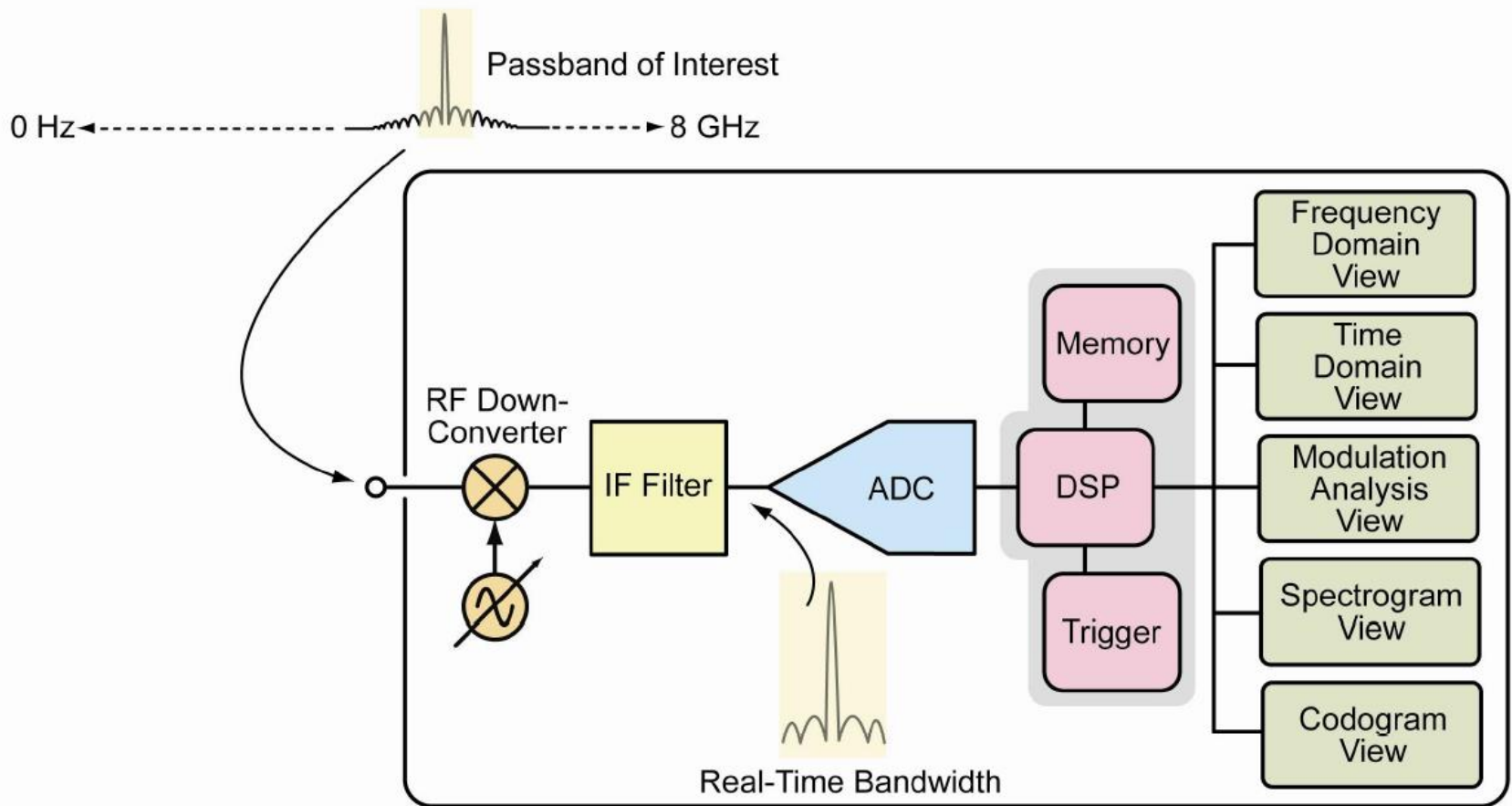
# Modern Spectrum Analyzer: Digital Receiver



# Modern SA block diagram



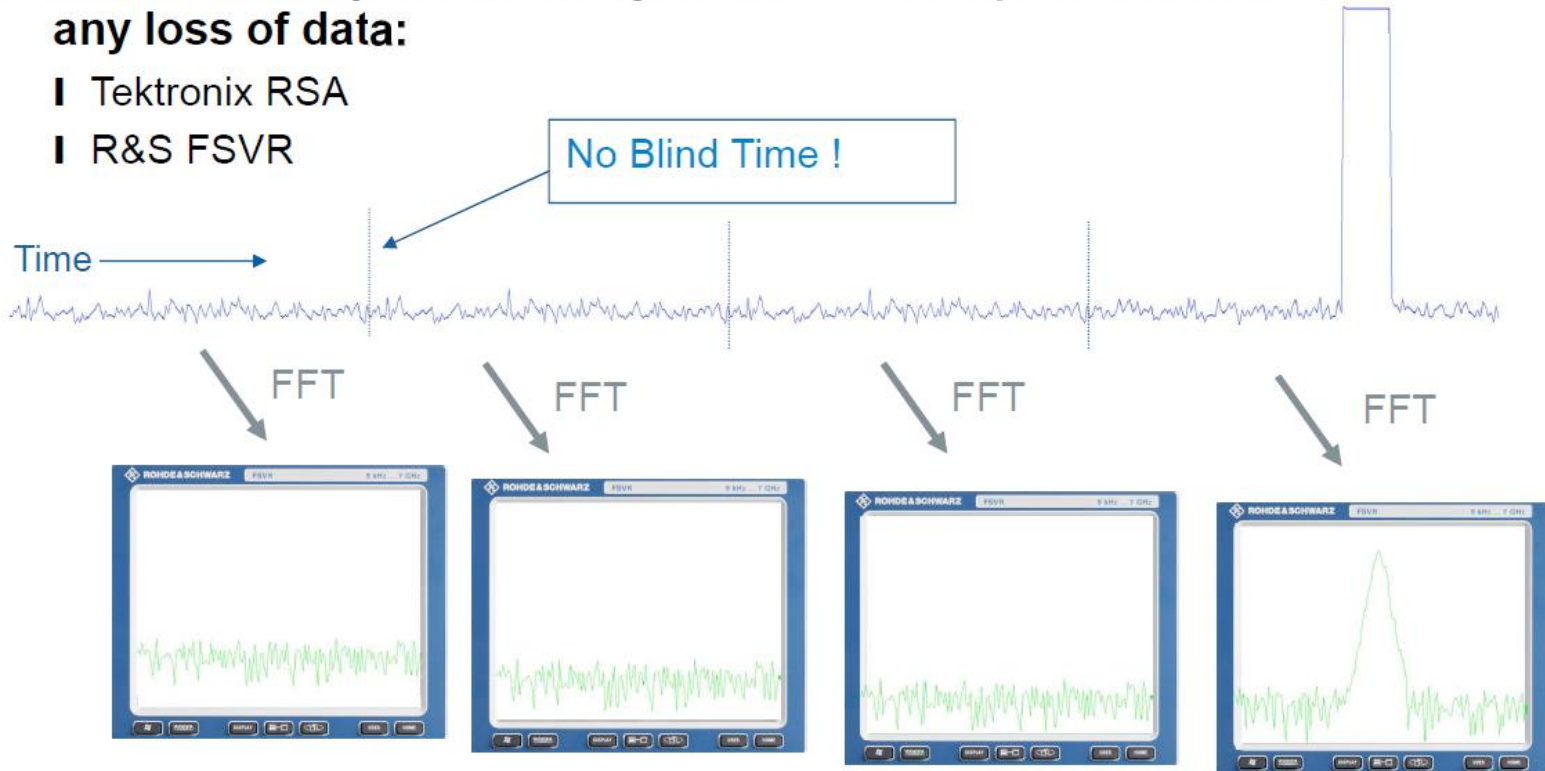
# Real-time Architecture



# Real-Time

I A Real-Time spectrum analyzer shows the spectrum without any loss of data:

- I Tektronix RSA
- I R&S FSVR



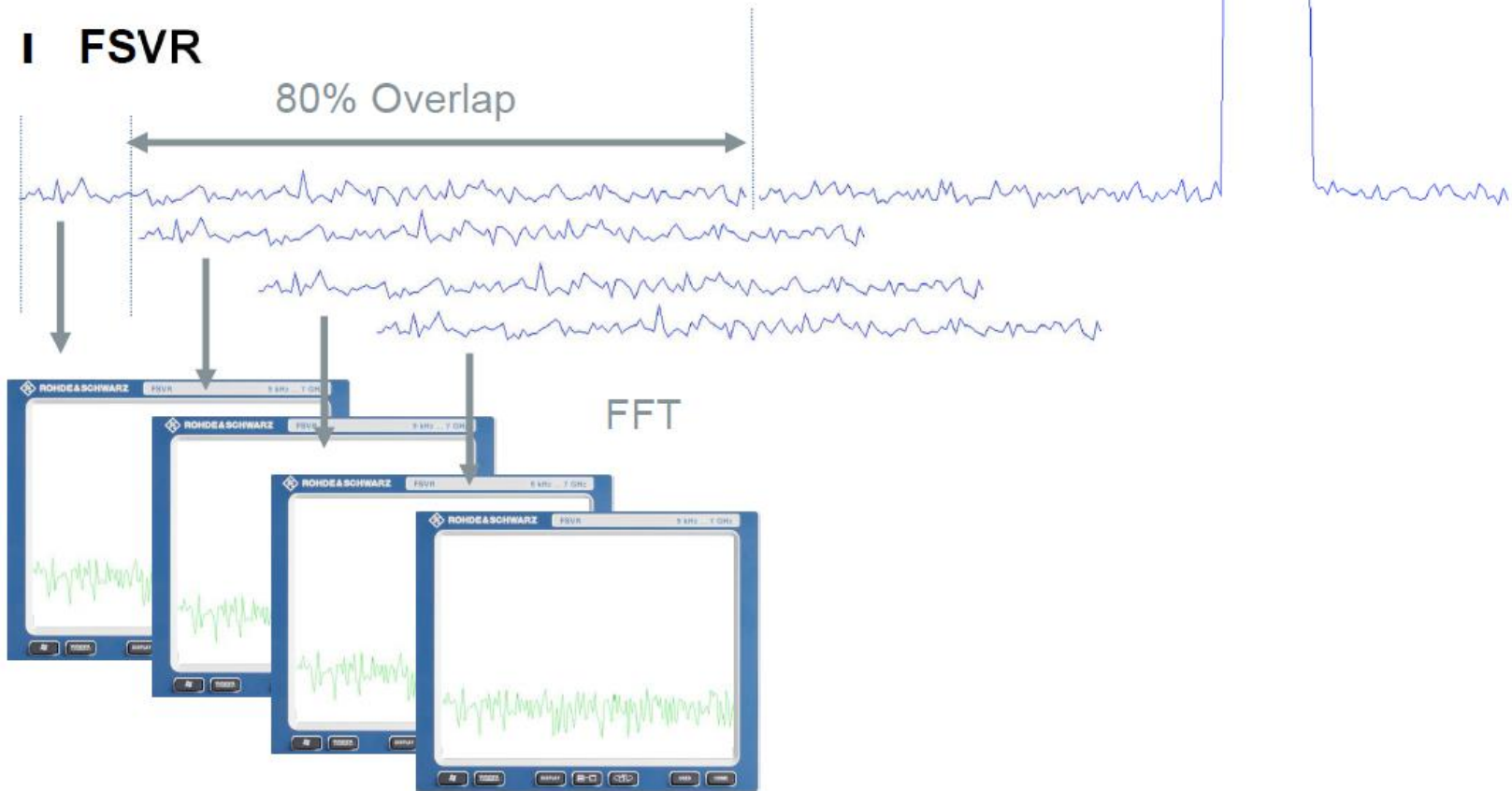


# Real-Time

## What is Real-Time – Overlap of FFTs

I FSVR

80% Overlap



# Measurement Time

The system is no-more swept: the local oscillator is at a fixed frequency and the frequency measurement is made by an FFT technique.

If  $SPAN < RTB$  (real time bandwidth), the measurement time is limited by the frequency resolution:

$$\text{Acquisition time} = T = 1 / RBW$$

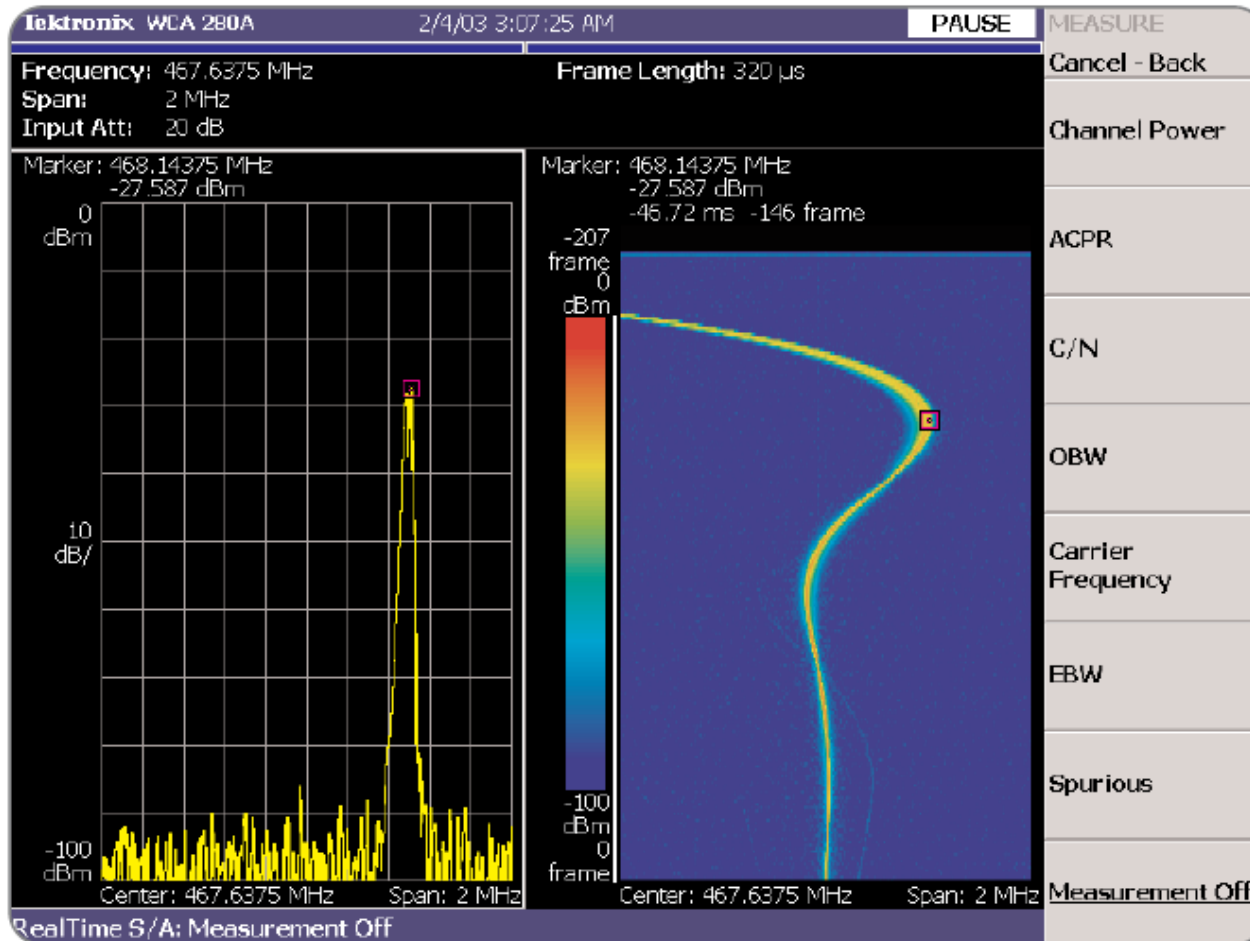
We have to consider also the time needed for the FFT elaboration, but it is often negligible (and some FFTs are made in parallel)

If  $SPAN > RTB$ , the local oscillator is moved for discrete steps, and the screen spectrum is a collage of some FFT results (no more phase coherence in the whole spectrum)

$$\text{Screen time} = SPAN / RTB \times (1 / RBW)$$

*For low RBW values it is much faster than swept analyzer ( $ST \cong 3SPAN / RTB^2$ )*

# New measurement possibilities



- **Figure 8.** Analysis of phase-locked loop. Spectrogram (right display) captures PLL response as it settles over time (top to bottom). Vertical axis is Time, horizontal axis is Frequency, and Power Density is represented by color.

